

PCFGs: Parsing & Evaluation

LING 571 — Deep Processing Techniques for NLP

October 9, 2019

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Roadmap

- Recap:
 - CKY + back-pointers
 - PCFGs
- PCFG Parsing (PCKY)
- Inducing a PCFG
- Evaluation
- [Earley parsing]
- HW3 + collaboration

CKY Follow-up: Backpointers

Backpointers

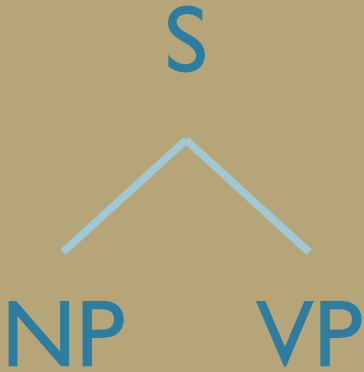
- Instead of list of possible nonterminals for that node, each cell should have:
 - Nonterminal for the node
 - Pointer to left and right children cells
 - Either direct pointer to cell, or indices

For example:

```
bp_2 = BackPointer()  
bp_2.l_child = [X2, (1,4)]  
bp_2.r_child = [PP, (4,6)]
```

cky_table[0,6][S] = {(NP, (0,1)),
VP, (1,6))}

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	S [0,6]
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP, X2, S [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



I

prefer

a

flight

on

TWA

$S[S] = \{ (NP, ($
VP, (

S

NP VP

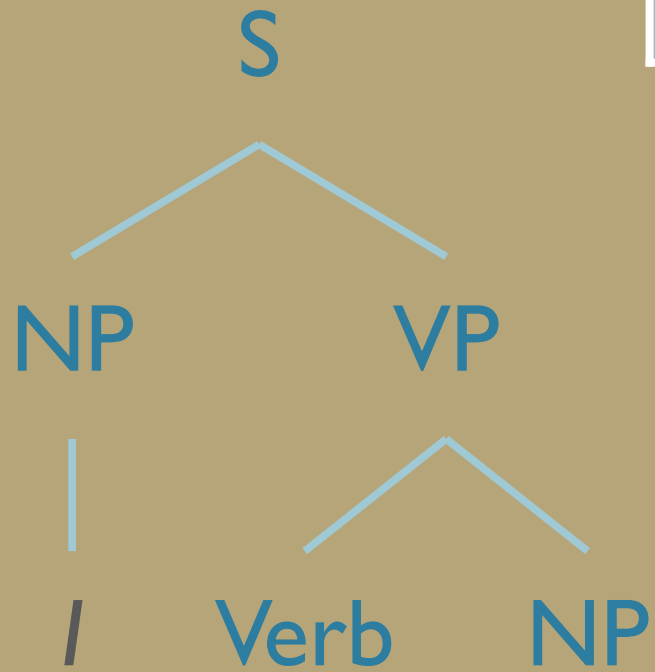
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I prefer a flight on TWA

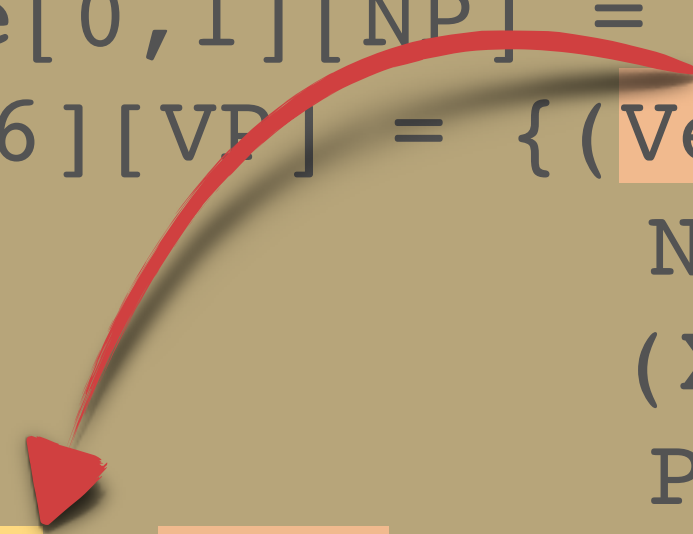
```
cky_table[0,6][S] = {(NP, (0,1)),
                    (VP, (1,6))}
cky_table[0,1][NP] = {('I')}
cky_table[1,6][VP] = {(Verb, (1,2)),
                    (NP, (2,6)),
                    (X2, (1,4)),
                    (PP, (4,6))}
```

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	S [0,6]
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP, X2, S [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]

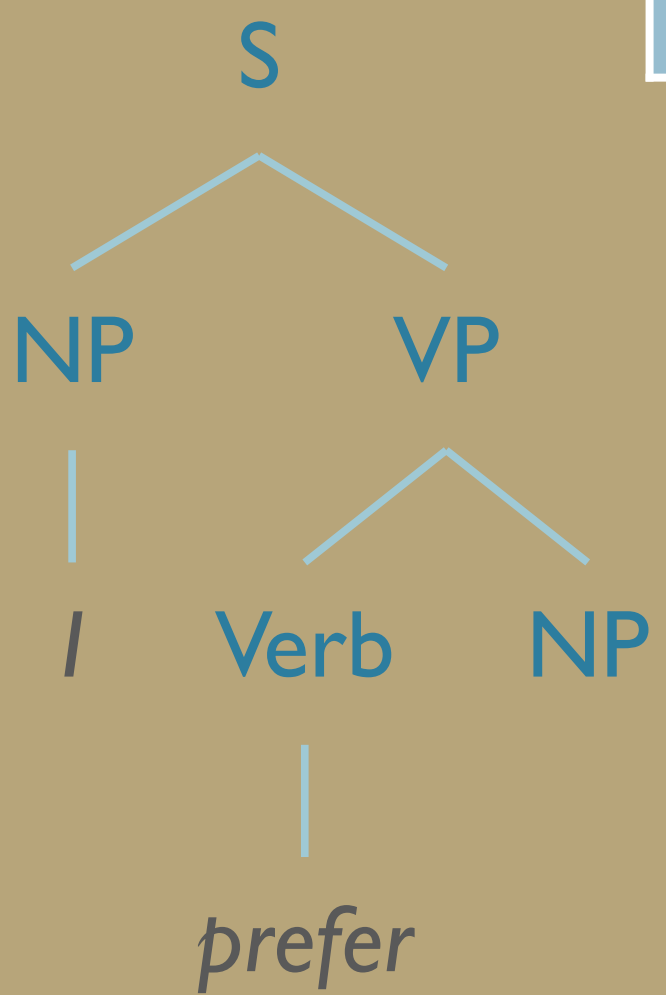


I prefer a flight on TWA

```
cky_table[0,6][S] = {(NP, (0,1),  
                      VP, (1,6))}  
cky_table[0,1][NP] = {('I')}  
cky_table[1,6][VP] = {(Verb, (1,2),  
                      NP, (2,6)),  
                      (X2, (1,4),  
                      PP, (4,6))}  
cky_table[1,2][Verb] = {('prefer')}
```



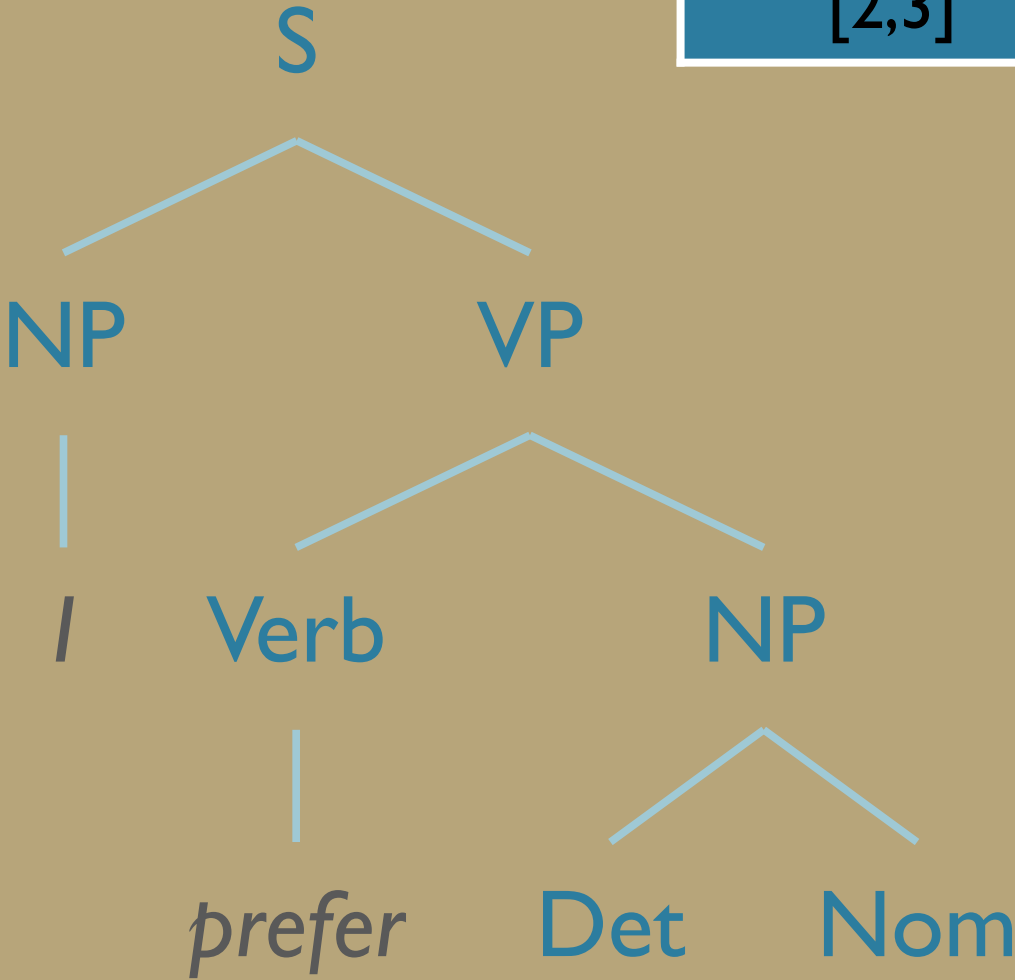
NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	S [0,6]
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP, X2, S [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



I prefer a flight on TWA


```
cky_table[0,6][S] = {(NP, (0,1)),
                    (VP, (1,6))}
cky_table[0,1][NP] = {'I'}
cky_table[1,6][VP] = {(Verb, (1,2)),
                    (NP, (2,6)),
                    (X2, (1,4)),
                    (PP, (4,6))}
cky_table[1,2][Verb] = {'prefer'}
cky_table[2,6][NP] = {(Det, (2,3)),
                    (Nom, (3,6))}
```

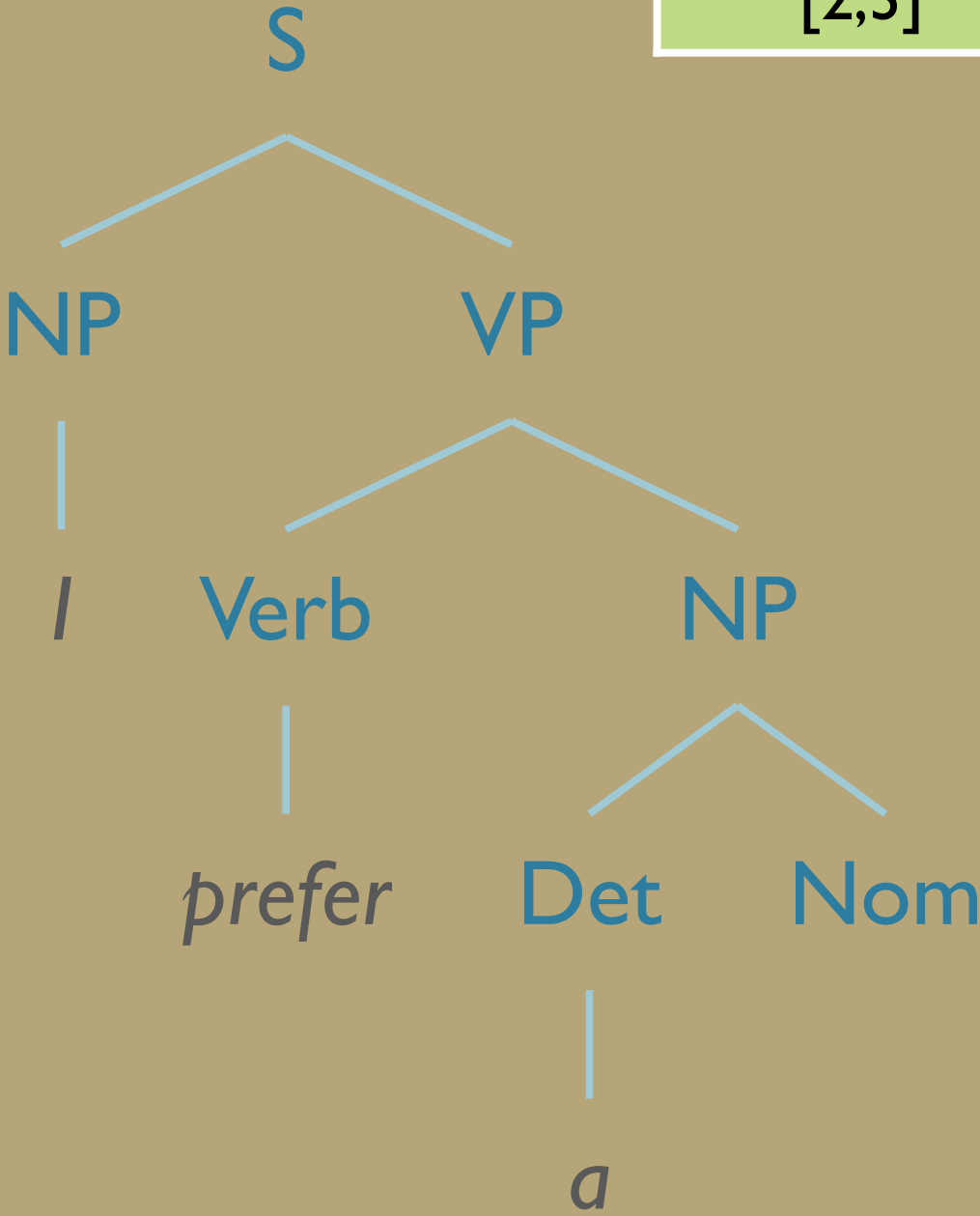
NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	S [0,6]
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP, X2, S [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



I prefer a flight on TWA

```
cky_table[0,6][S] = {(NP, (0,1),
                        VP, (1,6))}
cky_table[0,1][NP] = {('I')}
cky_table[1,6][VP] = {(Verb, (1,2),
                        NP, (2,6)),
                      (X2, (1,4),
                        PP, (4,6))}
cky_table[1,2][Verb] = {('prefer')}
cky_table[2,6][NP] = {(Det, (2,3),
                      Nom, (3,6))}
cky_table[2,3][Det] = {('a')}
```

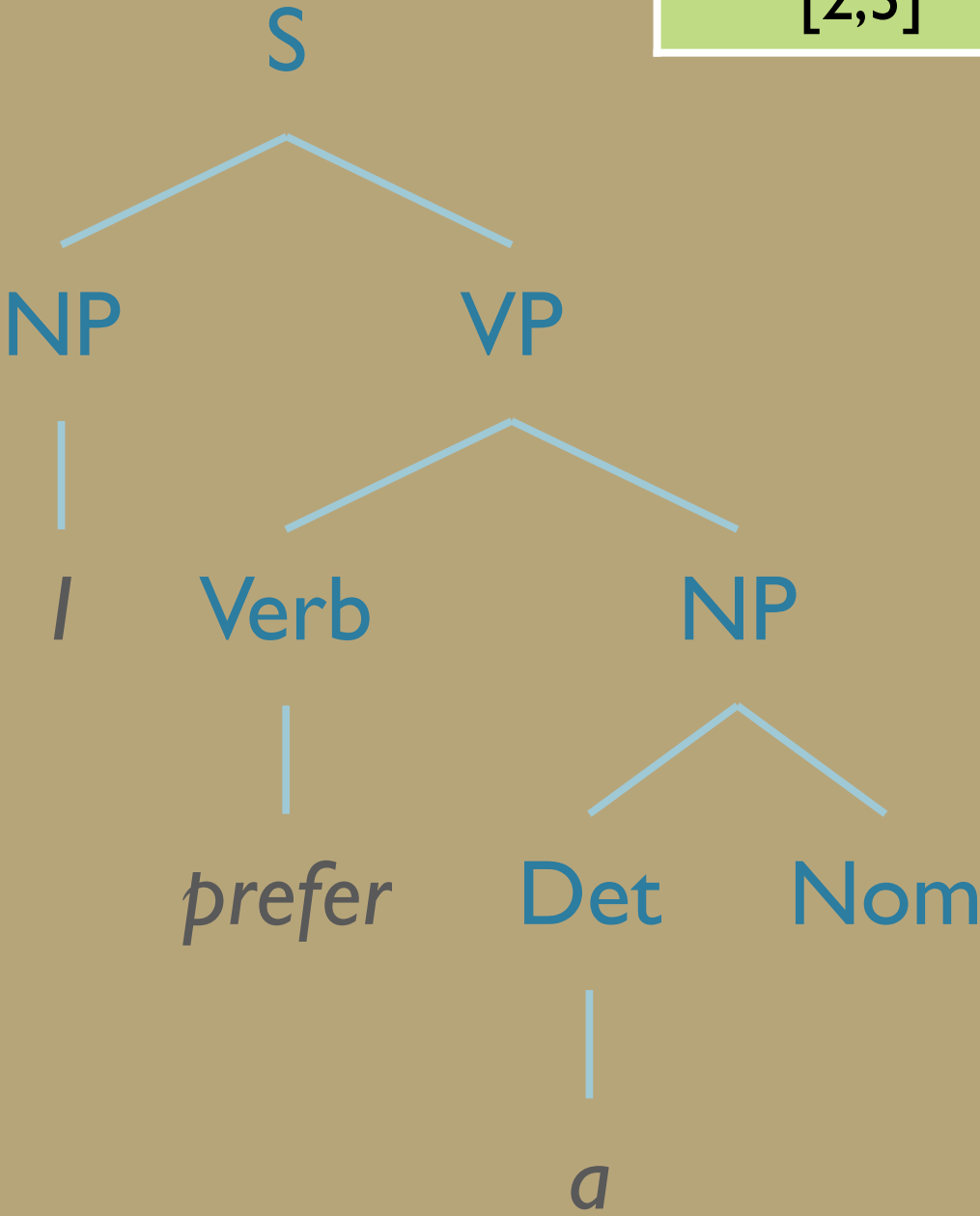
NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	S [0,6]
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP, X2, S [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



I prefer a flight on TWA

```
cky_table[0,6][S] = {(NP, (0,1),
                        VP, (1,6))}
cky_table[0,1][NP] = {'I'}
cky_table[1,6][VP] = {(Verb, (1,2),
                        NP, (2,6)),
                      (X2, (1,4),
                        PP, (4,6))}
cky_table[1,2][Verb] = {'prefer'}
cky_table[2,6][NP] = {(Det, (2,3),
                        Nom, (3,6))}
cky_table[2,3][Det] = {'a'}
```

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	S [0,6]
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP, X2, S [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]

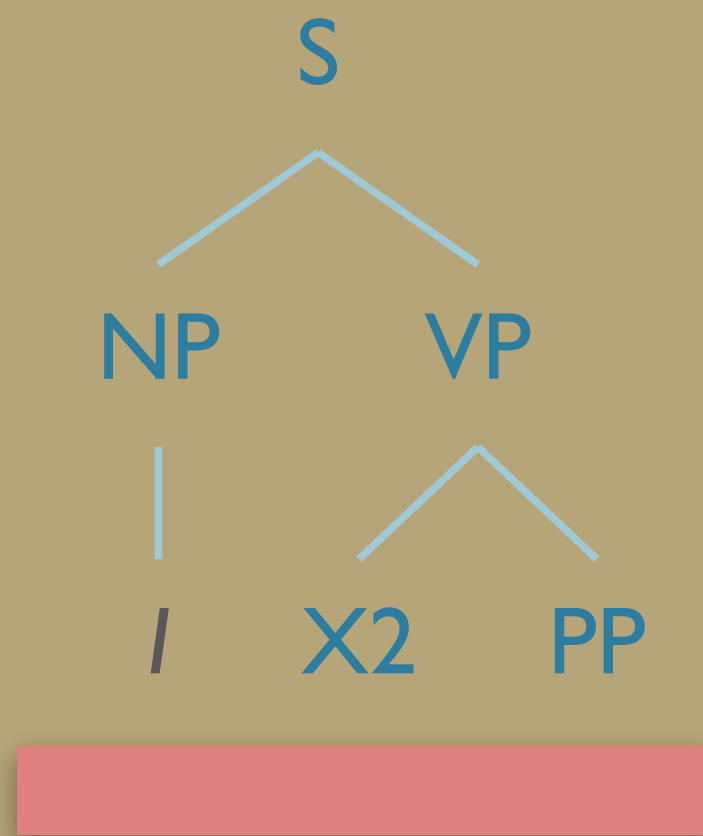
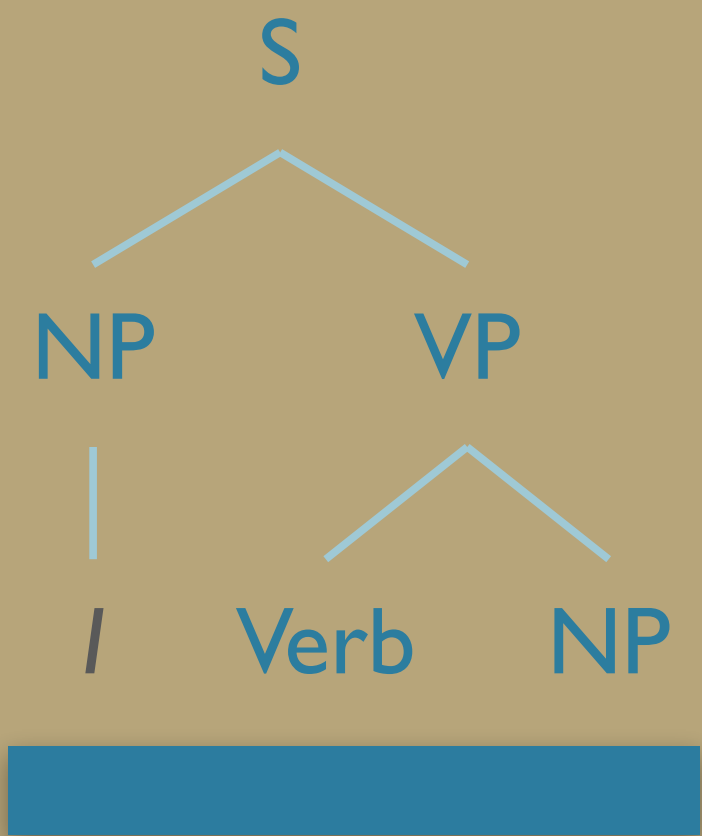


Exercise: finish the parse!

I prefer a flight on TWA

```
cky_table[0,6][S] = {(NP, (0,1)),
                    (VP, (1,6))}
cky_table[0,1][NP] = {'I'}
cky_table[1,6][VP] = {(Verb, (1,2)),
                    (NP, (2,6)),
                    (X2, (1,4)),
                    (PP, (4,6))}
```

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	S [0,6]
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP, X2, S [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



I prefer a flight on TWA

PCFGs: Recap

PCFGs: Formal Definition

N	a set of non-terminal symbols (or variables)
Σ	a set of terminal symbols (disjoint from N)
R	a set of rules of productions, each of the form $A \rightarrow \beta[p]$, where A is a non-terminal where A is a non-terminal, β is a string of symbols from the infinite set of strings $(\Sigma \cup N)^*$ and p is a number between 0 and 1 expressing $P(\beta A)$
S	a designated start symbol

Disambiguation

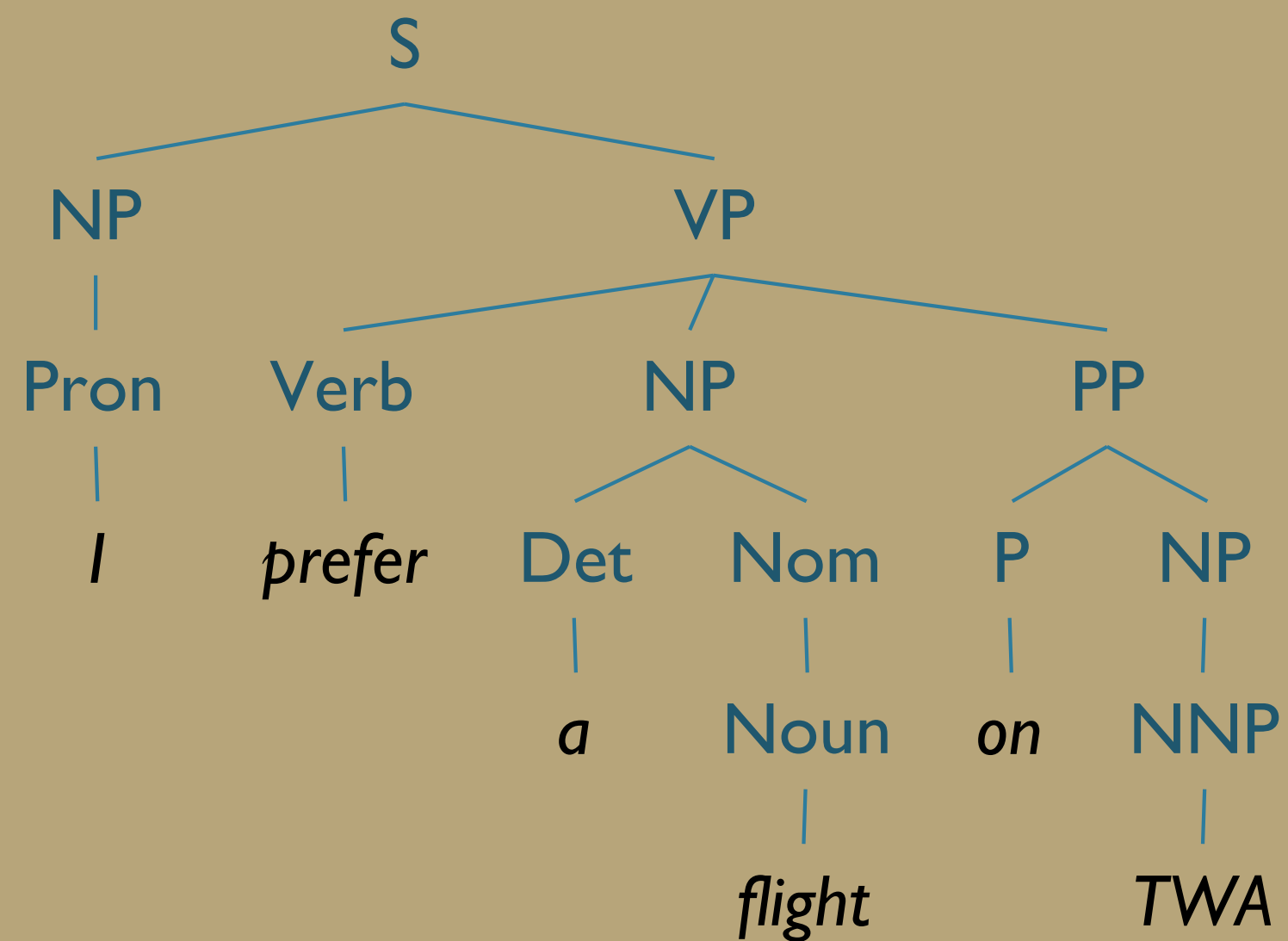
- A PCFG assigns probability to each parse tree T for input S
- Probability of T : product of all rules used to derive T

$$P(T, S) = \prod_{i=1}^n P(RHS_i | LHS_i)$$

$$P(T, S) = P(T) \cdot P(S | T) = P(T)$$

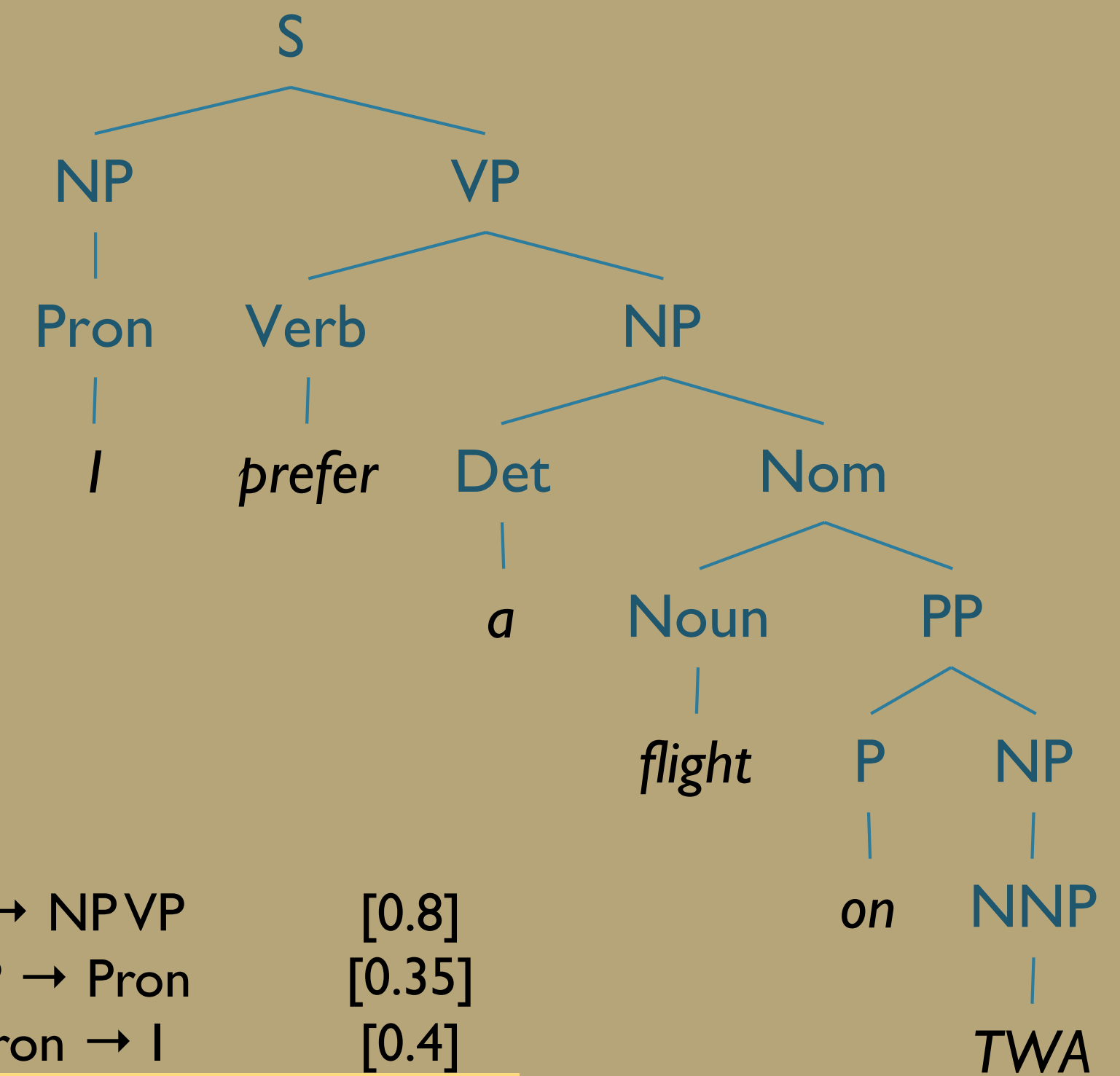
Application: Language Modeling

- n -grams helpful for modeling the probability of a string
- To model a whole sentence with n -grams either:
 - Must use 10+-grams... too sparse
 - Approximate using conditioning on limited context:
$$P(w_i | w_{i-1}) = \frac{P(w_{i-1}, w_i)}{P(w_{i-1})}$$
- PCFGs are able to give probability of entire string without as bad sparsity
- Model probability of *syntactically valid* sentences
 - Not just probability of sequence of words



$S \rightarrow NPVP$	[0.8]
$NP \rightarrow Pron$	[0.35]
$Pron \rightarrow I$	[0.4]
$VP \rightarrow V NP PP$	[0.1]
$V \rightarrow prefer$	[0.4]
$NP \rightarrow Det Nom$	[0.2]
$Det \rightarrow a$	[0.3]
$Nom \rightarrow N$	[0.75]
$N \rightarrow flight$	[0.3]
$PP \rightarrow P NP$	[1.0]
$P \rightarrow on$	[0.2]
$NP \rightarrow NNP$	[0.3]
$NNP \rightarrow NWA$	[0.4]

$\sim 1.452 \times 10^{-6}$



$S \rightarrow NPVP$	[0.8]
$NP \rightarrow Pron$	[0.35]
$Pron \rightarrow I$	[0.4]
$VP \rightarrow V NP$	[0.2]
$V \rightarrow prefer$	[0.4]
$NP \rightarrow Det Nom$	[0.2]
$Det \rightarrow a$	[0.3]
$Nom \rightarrow Nom PP$	[0.05]
$Nom \rightarrow N$	[0.75]
$N \rightarrow flight$	[0.3]
$PP \rightarrow P NP$	[1.0]
$P \rightarrow on$	[0.2]
$NP \rightarrow NNP$	[0.3]
$NNP \rightarrow NWA$	[0.4]

$\sim 1.452 \times 10^{-7}$

Parsing Problem for PCFGs

- Select T such that *(s.t.)*

$$\hat{T}(S) = \underset{T \text{ s.t. } S = \text{yield}(T)}{\operatorname{argmax}} P(T)$$

- String of words S is *yield* of parse tree
- Select the tree \hat{T} that maximizes the probability of the parse
- Extend existing algorithms: e.g. CKY

PCFGs: Parsing

Probabilistic CKY (PCKY)

- Like regular CKY
 - Assumes grammar in Chomsky Normal Form (CNF)
 - $A \rightarrow B C$
 - $A \rightarrow w$
 - Represent input with indices b/t words:
 - $_0 \text{ Book } _1 \text{ that } _2 \text{ flight } _3 \text{ through } _4 \text{ Houston } _5$

Probabilistic CKY (PCKY)

- For input string length n and non-terminals V
 - Cell $[i, j, A]$ in $(n+1) \times (n+1) \times V$ matrix
 - Contains probability that A spans $[i, j]$

PCKY Algorithm

```
function PROBABILISTIC-CKY-PARSE(words, grammar) returns most probable parse and its probability
for j ← from 1 to LENGTH(words) do
  for all { A |  $A \rightarrow words[j] \in grammar$  }
     $table[j-1, j, A] \leftarrow P(A \rightarrow words[j])$ 
  for i ← from j-2 downto 0 do
    for k ← i + 1 to j-1 do
      for all { A |  $A \rightarrow B C \in grammar$ ,
        and  $table[i, k, B] > 0$  and  $table[k, j, C] > 0$  }
        if ( $table[i, j, A] < P(A \rightarrow BC) \times table[i, k, B] \times table[k, j, C]$ ) then
           $table[i, j, A] \leftarrow P(A \rightarrow BC) \times table[i, k, B] \times table[k, j, C]$ 
           $back[i, j, A] \leftarrow \{ k, B, C \}$ 
  return BUILD_TREE( $back[1, LENGTH(words), S]$ ),  $table[1, LENGTH(words), S]$ 
```

PCKY Grammar Segment

$S \rightarrow NP VP$ [0.80]

$NP \rightarrow Det N$ [0.30]

$VP \rightarrow V NP$ [0.20]

$Det \rightarrow the$ [0.40]

$Det \rightarrow a$ [0.40]

$V \rightarrow includes$ [0.05]

$N \rightarrow meal$ [0.01]

$N \rightarrow flight$ [0.02]

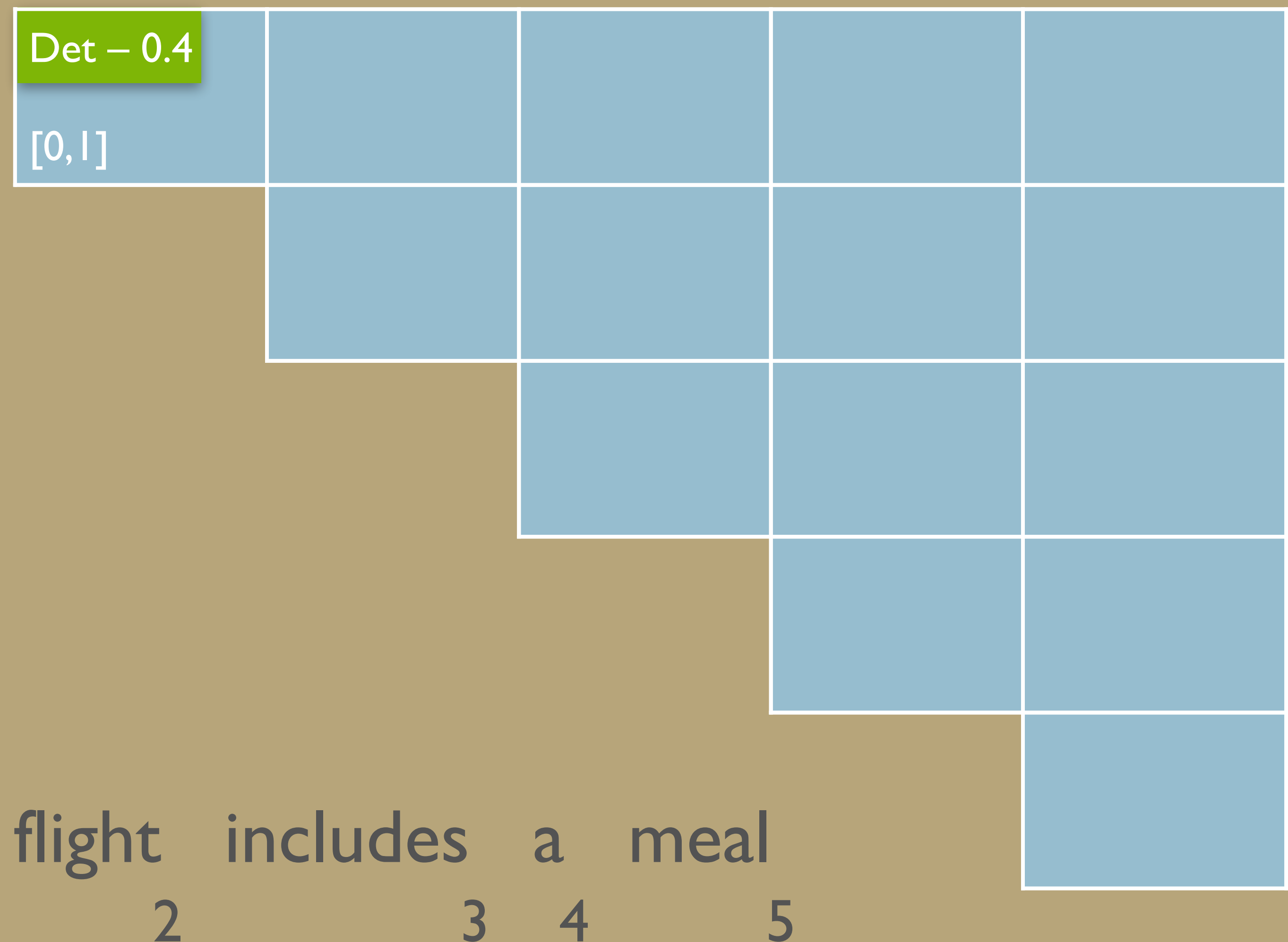
PCKY Matrix

$$S \rightarrow NP \ VP \quad [0.80]$$
$$NP \rightarrow Det\ N \quad [0.30]$$
$$VP \rightarrow V NP \quad [0.20]$$

Det → the [0.40]

$$Det \rightarrow \mathfrak{a} \quad [0.40]$$

$V \rightarrow$ includes $[0.05]$

$$N \rightarrow \text{meal} \quad [0.01]$$
$$N \rightarrow \text{flight} \quad [0.02]$$


PCKY Matrix

$$S \rightarrow NP \ VP \quad [0.80]$$
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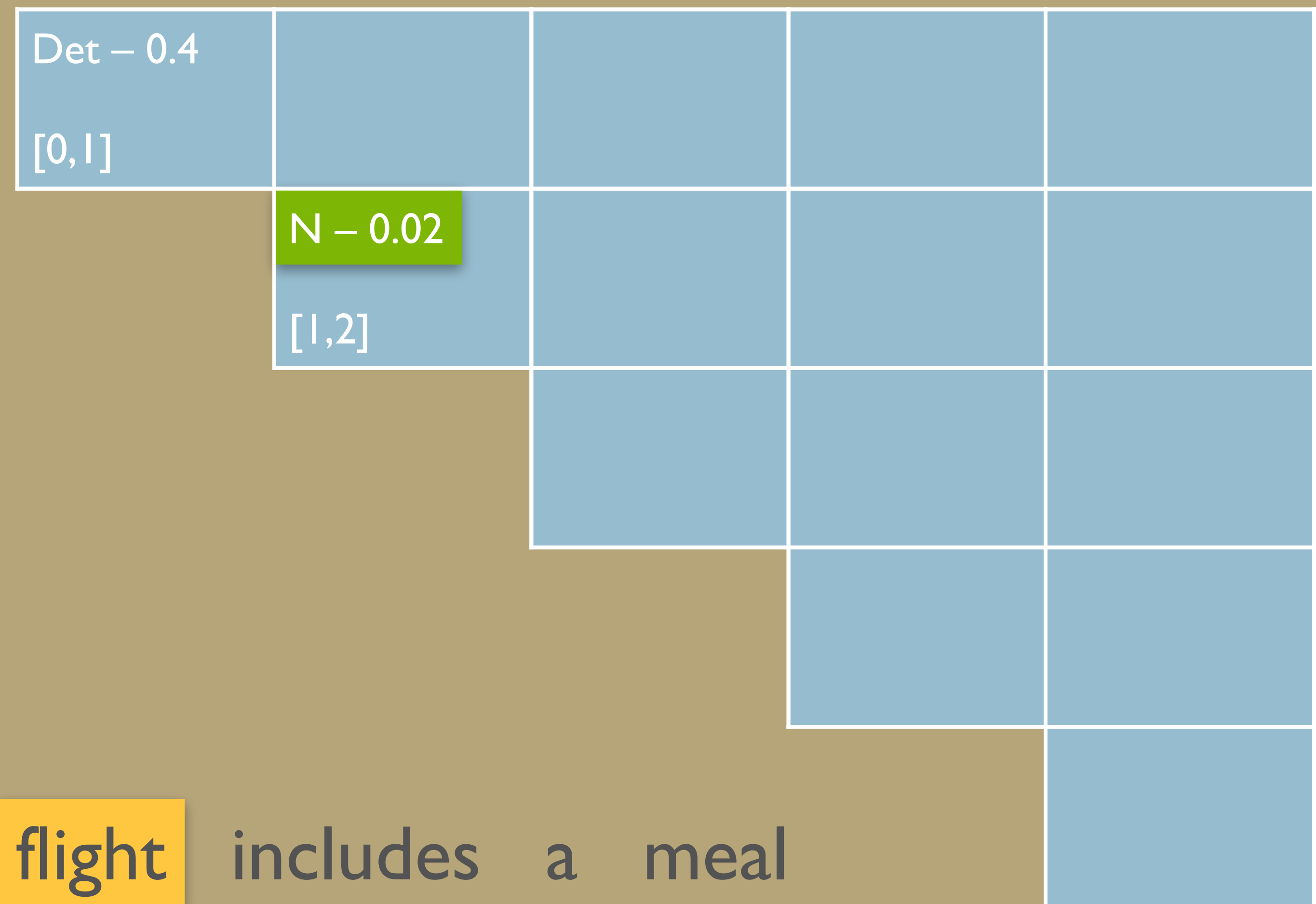
Det → the [0.40]

$$Det \rightarrow a \quad [0.40]$$

$V \rightarrow$ includes $[0.05]$

$$N \rightarrow \text{meal} \quad [0.01]$$

$N \rightarrow \text{flight} \quad [0.02]$



0 1 2 3 4 5

PCKY Matrix

$$S \rightarrow NP \ VP \quad [0.80]$$

$NP \rightarrow Det N$ [0.30]

$$VP \rightarrow V NP \quad [0.20]$$

$Det \rightarrow$ the [0.40]

$$Det \rightarrow a \quad [0.40]$$

$V \rightarrow$ includes $[0.05]$

$$N \rightarrow \text{meal} \quad [0.01]$$

$N \rightarrow \text{flight}$ [0.02]

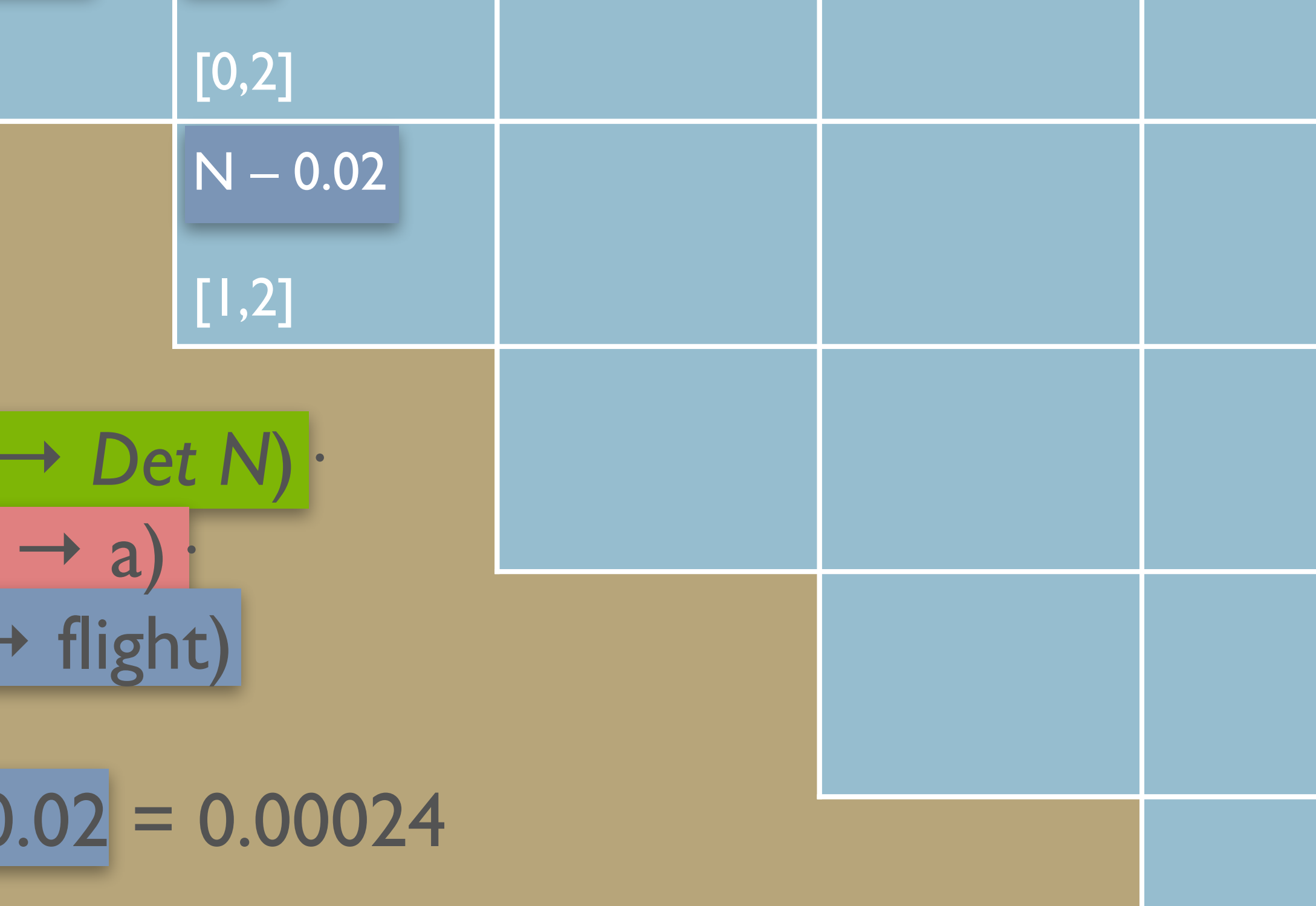


Diagram illustrating the joint probability calculation for the sentence "flight includes a meal" using a Naive Bayes model. The diagram shows a grid of cells representing the joint probability distribution over the words and their parts of speech. The cells are colored blue, green, and red, corresponding to the parts of speech: NP (green), Det (red), and N (blue). The grid is divided into three sections: the top-left section shows the joint probability distribution for the words "flight" and "includes", the middle section shows the joint probability distribution for the words "a" and "meal", and the bottom-right section shows the joint probability distribution for the words "flight" and "meal".

Top-left section (flight, includes):

- Det (red): 0.4
- NP (green): 0.02
- N (blue): 0.02

Middle section (a, meal):

- Det (red): 0.4
- NP (green): 0.02
- N (blue): 0.02

Bottom-right section (flight, meal):

- Det (red): 0.4
- NP (green): 0.02
- N (blue): 0.02

Calculation:

$$0.4 \cdot 0.02 = 0.00024$$

flight includes a meal

$$P = P(NP \rightarrow Det\ N) \cdot P(Det \rightarrow a) \cdot P(N \rightarrow flight)$$

$$P = 0.3 \cdot 0.4 \cdot 0.02 = 0.00024$$

The flight includes a meal

PCKY Matrix

$$S \rightarrow NP \ VP \quad [0.80]$$

$NP \rightarrow Det N$ [0.30]

$$VP \rightarrow V NP \quad [0.20]$$

$Det \rightarrow$ the [0.40]

$Det \rightarrow a$ [0.40]

$V \rightarrow$ includes $[0.05]$

$$N \rightarrow \text{meal} \quad [0.01]$$
$$N \rightarrow \text{flight} \quad [0.02]$$
$$P = P(NP \rightarrow Det\ N) \cdot P(Det \rightarrow a) \cdot P(N \rightarrow flight)$$

$$P = 0.3 \cdot 0.4 \cdot 0.02 = 0.00024$$

The flight includes a meal

0



2

3

4

5

PCKY Matrix

$S \rightarrow NP VP$ [0.80]
 $NP \rightarrow Det N$ [0.30]
 $VP \rightarrow V NP$ [0.20]

$Det \rightarrow the$ [0.40]
 $Det \rightarrow a$ [0.40]
 $V \rightarrow includes$ [0.05]
 $N \rightarrow meal$ [0.01]
 $N \rightarrow flight$ [0.02]

Det – 0.4 [0,1]	NP – 0.0024 [0,2]			S – 2.304×10 ⁻⁸ [0,5]
	N – 0.02 [1,2]			
		V – 0.05 [2,3]		VP – 1.2×10 ⁻⁵ [2,5]
			Det – 0.4 [3,4]	NP – 0.0012 [3,5]
				N – 0.01 [4,5]

0 1 2 3 4 5
The flight includes a meal

Inducing a PCFG

Learning Probabilities

- Simplest way:
 - Use treebank of parsed sentences
 - To compute probability of a rule, count:
 - Number of times a nonterminal is expanded:
 - Number of times a nonterminal is expanded by a given rule:

$$\frac{\sum_{\gamma} \text{Count}(\alpha \rightarrow \gamma)}{\text{Count}(\alpha \rightarrow \beta)}$$

$$P(\alpha \rightarrow \beta \mid \alpha) = \frac{\text{Count}(\alpha \rightarrow \beta)}{\sum_{\gamma} \text{Count}(\alpha \rightarrow \gamma)} = \frac{\text{Count}(\alpha \rightarrow \beta)}{\text{Count}(\alpha)}$$

- Alternative: Learn probabilities by re-estimating
 - (Later)

Probabilistic Parser Development Paradigm

	Train	Dev	Test
Size	Large (eg. WSJ 2–21, 39,830 sentences)	Small (e.g. WSJ 22)	Small/Med (e.g. WSJ, 23, 2,416 sentences)
Usage	Estimate rule probabilities	Tuning/Verification, Check for Overfit	Held Out, Final Evaluation

Parser Evaluation

Parser Evaluation

- Assume a ‘gold standard’ set of parses for test set
- How can we tell how good the parser is?
- How can we tell how good a parse is?
 - Maximally strict: identical to ‘gold standard’
 - Partial credit:
 - Constituents in output match those in reference
 - Same start point, end point, non-terminal symbol

Parseval

- How can we compute parse score from constituents?
- Multiple Measures:

$$\text{Labeled Recall (LR)} = \frac{\# \text{ of } \mathbf{correct} \text{ constituents in } \mathbf{hypothetical} \text{ parse}}{\# \text{ of } \mathbf{total} \text{ constituents in } \mathbf{reference} \text{ parse}}$$

$$\text{Labeled Precision (LP)} = \frac{\# \text{ of } \mathbf{correct} \text{ constituents in } \mathbf{hypothetical} \text{ parse}}{\# \text{ of } \mathbf{total} \text{ constituents in } \mathbf{hypothetical} \text{ parse}}$$

Parseval

- **F-measure:**

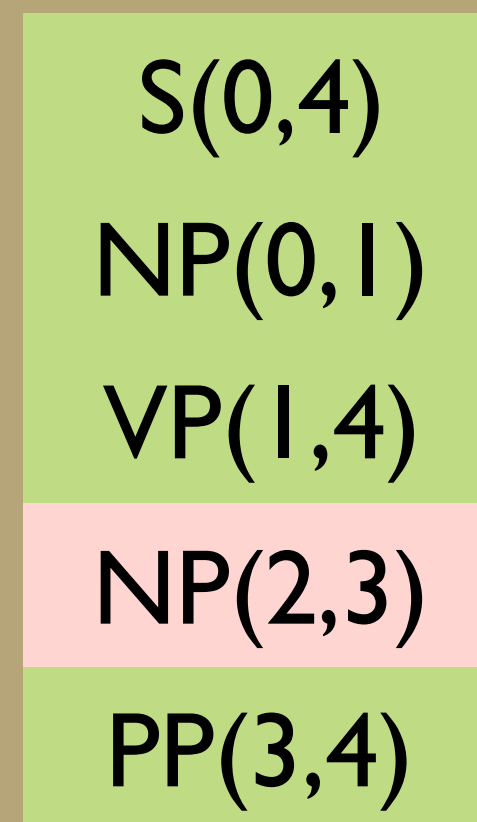
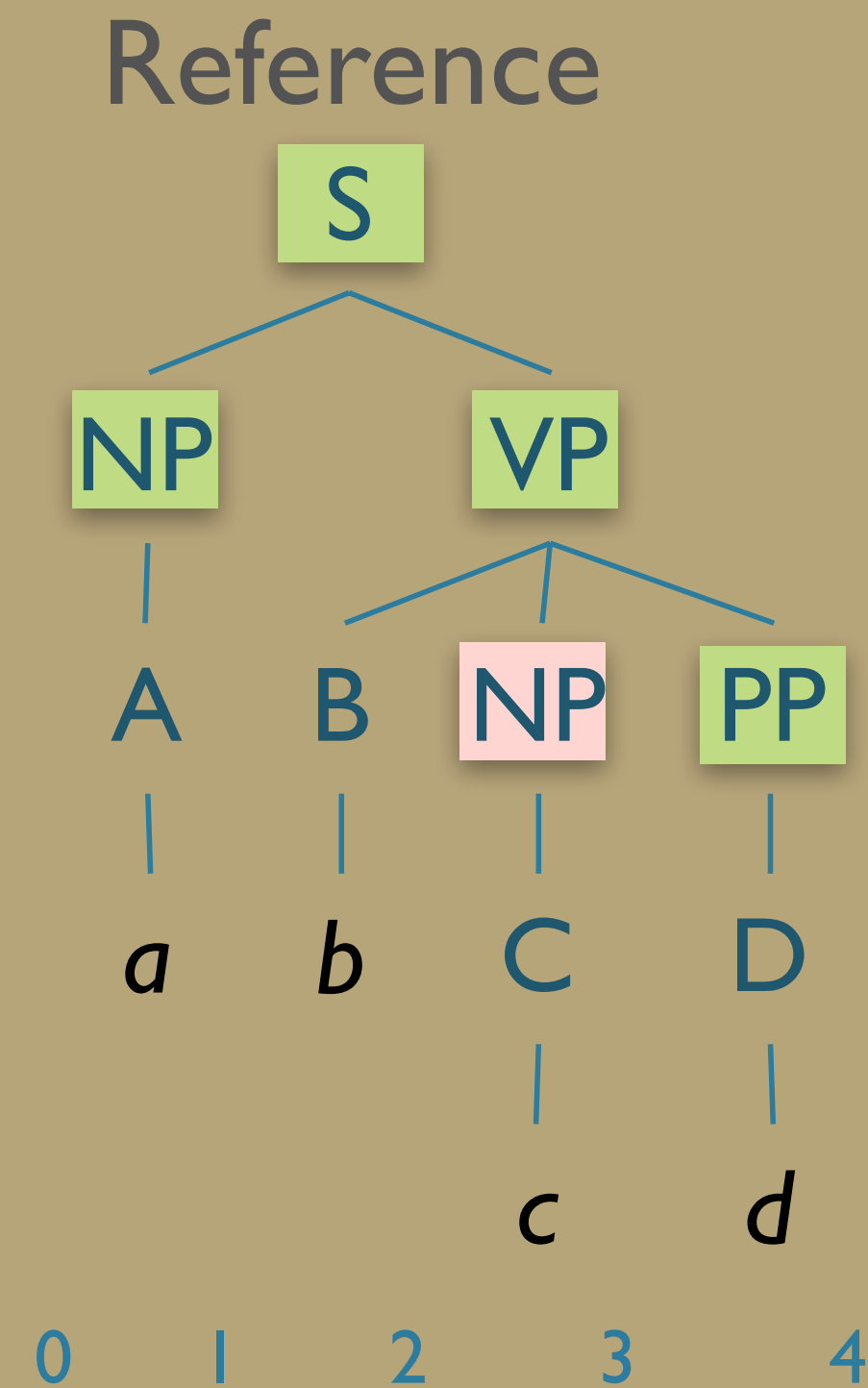
- Combines precision and recall

- Let $\beta \in \mathbb{R}$, $\beta > 0$ that adjusts P vs. R s.t. $\beta \propto \frac{R}{P}$

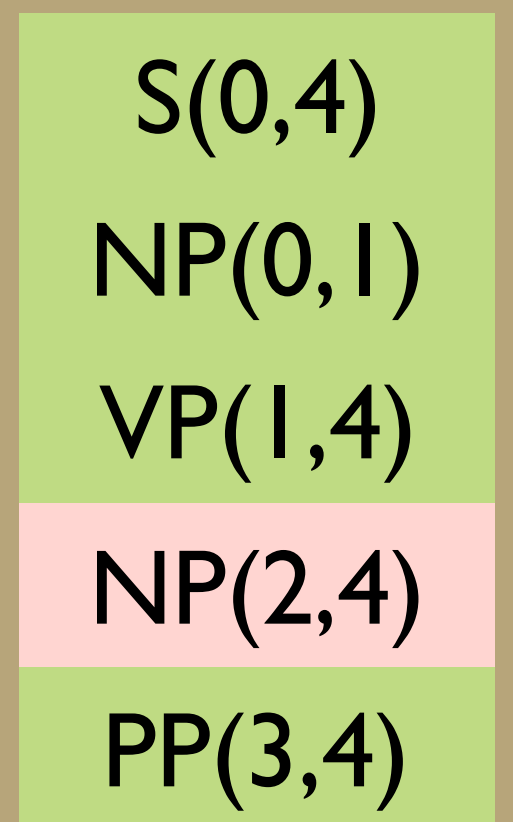
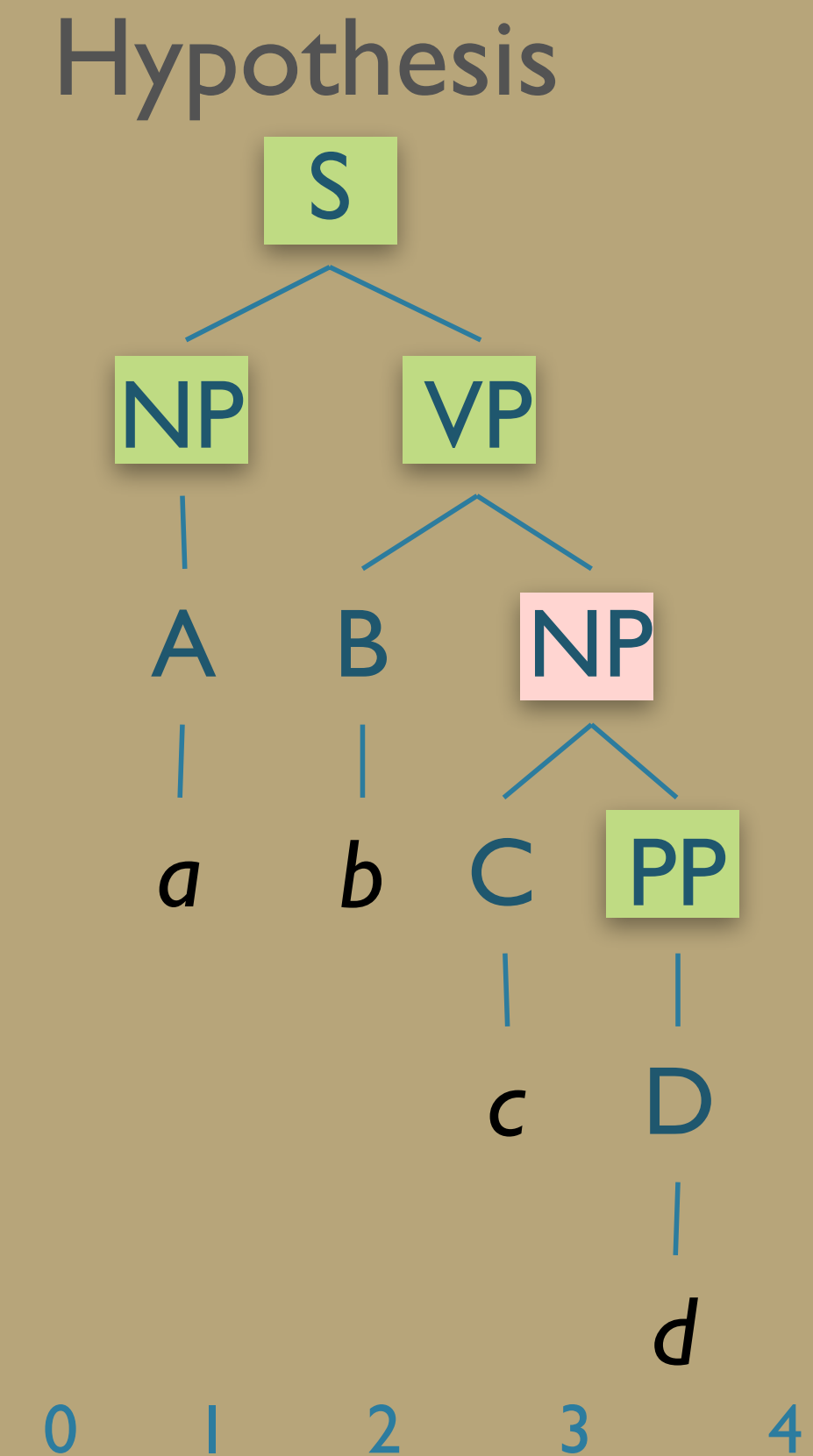
- F_β -measure is then:
$$F_\beta = (1 + \beta^2) \cdot \frac{P \cdot R}{\beta^2 \cdot P + R}$$

- With F1-measure as
$$F_1 = \frac{2PR}{P + R}$$

Evaluation: Example

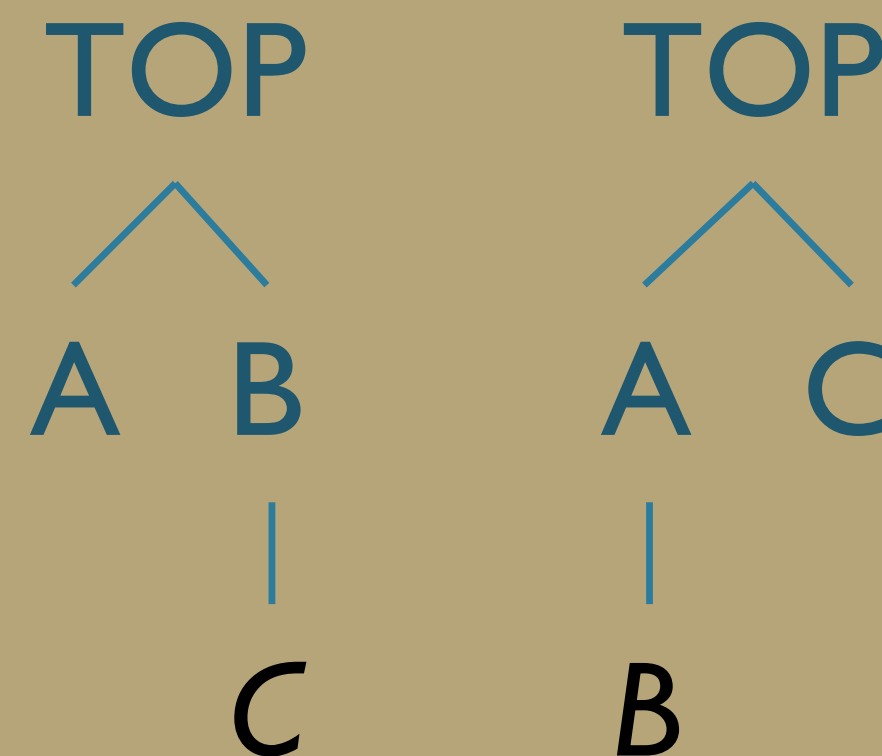


LP: 4/5
LR: 4/5
F₁: 4/5



Parser Evaluation

- Crossing Brackets:
 - # of constituents where produced parse has bracketings that overlap for the siblings:
 - ((A B) C) — { (0,2), (2,3) }
and hyp. has
(A (B C)) — { (0,1), (1, 3) }



```
/* crossing is counted based on the brackets */
/* in test rather than gold file (by Mike) */
for(j=0;j<bn2;j++){
  for(i=0;i<bn1;i++){
    if(bracket1[i].result != 5 &&
       bracket2[j].result != 5 &&
       ((bracket1[i].start < bracket2[j].start &&
         bracket1[i].end > bracket2[j].start &&
         bracket1[i].end < bracket2[j].end) ||
        (bracket1[i].start > bracket2[j].start &&
         bracket1[i].start < bracket2[j].end &&
         bracket1[i].end > bracket2[j].end))){
```

from evalb.c

State-of-the-Art Parsing

- Parsers trained/tested on Wall Street Journal PTB
 - LR: 90%+;
 - LP: 90%+;
 - Crossing brackets: 1%
- Standard implementation of Parseval:
 - **evalb**

Evaluation Issues

- Only evaluating constituency
- There are other grammar formalisms:
 - LFG (Constraint-based)
 - Dependency Structure
- **Extrinsic** evaluation
 - How well does getting the correct parse match the semantics, etc?

Earley Parsing

Earley vs. CKY

- CKY doesn't capture full original structure
 - Can back-convert binarization, terminal conversion
 - Unit non-terminals require change in CKY
- Earley algorithm
 - Supports parsing efficiently with arbitrary grammars
 - Top-down search
 - Dynamic programming
 - Tabulated partial solutions
 - Some bottom-up constraints

Earley Algorithm

- Another dynamic programming solution
 - Partial parses stored in “chart”
 - Compactly encodes ambiguity
 - $O(N^3)$
- Chart entries contain:
 - Subtree for a single grammar rule
 - Progress in completing subtree
 - Position of subtree w.r.t. input

Earley Algorithm

- First, left-to-right pass fills out a chart with $N+1$ states
 - Chart entries — sit between words in the input string
 - Keep track of states of the parse at those positions
 - For each word position, chart contains set of states representing all partial parse trees generated so far
 - e.g. `chart[0]` contains all partial parse trees generated at the beginning of sentence

Chart Entries

- Three types of constituents:
 - Predicted constituents
 - In-progress constituents
 - Completed constituents

Parse Progress

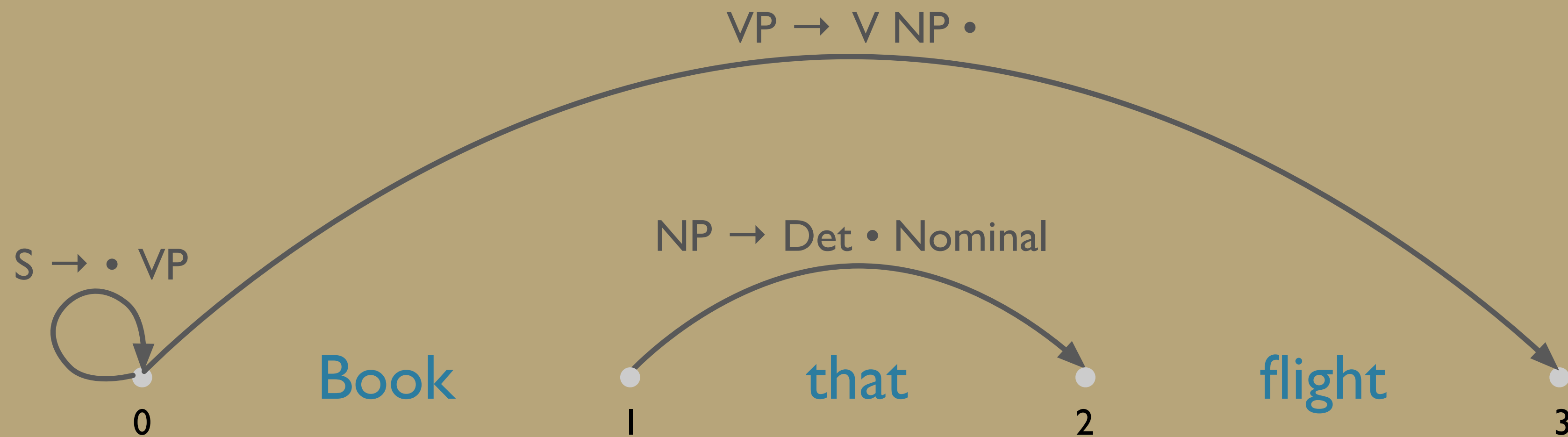
- Represented by Dotted Rules
 - Position of • indicates type of constituent
- $_0$ Book $_1$ that $_2$ flight $_3$
 - $S \rightarrow \bullet VP$ [0,0] (predicted)
 - $NP \rightarrow Det \bullet Nom$ [1,2] (in progress)
 - $VP \rightarrow V NP \bullet$ [0,3] (completed)
- [x,y] tells us what portion of the input is spanned so far by rule
- Each state s_i : <dotted rule>, [<back pointer>, <current position>]

₀ Book ₁ that ₂ flight ₃

- $S \rightarrow VP, [0,0]$
 - First 0 means S constituent begins at the start of input
 - Second 0 means the dot is here too
 - So, this is a top-down prediction
- $NP \rightarrow Det \cdot Nom, [1,2]$
 - the NP begins at position 1
 - the dot is at position 2
 - so, Det has been successfully parsed
 - Nom predicted next

$_0$ Book $_1$ that $_2$ flight $_3$ (continued)

- $V \rightarrow V NP \cdot [0,3]$
- Successful VP parse of entire input



Successful Parse

- Final answer found by looking at last entry in chart
- If entry resembles $S \rightarrow \alpha \cdot [0, N]$ then input parsed successfully
- Chart will also contain record of all possible parses of input string, given the grammar

Parsing Procedure for the Earley Algorithm

- Move through each set of states in order, applying one of three operations:
 - **predictor**: add predictions to the chart
 - **scanner**: read input and add corresponding state to chart
 - **completer**: move dot to right when new constituent found
- Results (new states) added to current or next set of states in chart
- No backtracking and no states removed: keep complete history of parse

Earley Algorithm

```
function EARLEY-PARSE(words, grammar) returns chart
  ENQUEUE( $(\gamma \longrightarrow \bullet S, [0,0])$ , chart[0])
  for  $i \longleftarrow$  from 0 to LENGTH(words) do
    for each state in chart[i] do
      if INCOMPLETE?(state) and
        NEXT-CAT(state) is not a part of speech then
        PREDICTOR(state)
      elseif INCOMPLETE?(state) and
        NEXT-CAT(state) is a part of speech then
        SCANNER(state)
      else
        COMPLETER(state)
    end
  end
  return(chart)
```

Earley Algorithm

```
procedure PREDICTOR(( $A \rightarrow a \bullet B \beta$ ,  $[i,j]$ ))  
  for each ( $B \rightarrow \gamma$ ) in GRAMMAR-RULES-FOR( $B, grammar$ ) do  
    ENQUEUE(( $B \rightarrow \bullet \gamma$ ,  $[j,j]$ ),  $chart[j]$ )  
  end
```

```
procedure SCANNER(( $A \rightarrow a \bullet B \beta$ ,  $[i,j]$ ))  
  if  $B \in \text{PARTS-OF-SPEECH}(word[j])$  then  
    ENQUEUE(( $B \rightarrow word[j] \bullet$ ,  $[j,j+1]$ ),  $chart[j+1]$ )
```

```
procedure COMPLETER(( $B \rightarrow \gamma \bullet$ ,  $[j,k]$ ))  
  for each ( $A \rightarrow a \bullet B \beta$ ,  $[i,j]$ ) in  $chart[j]$  do  
    ENQUEUE(( $A \rightarrow a B \bullet \beta$ ,  $[i,k]$ ),  $chart[k]$ )  
  end
```

3 Main Subroutines of Earley

- Predictor
 - Adds predictions into the chart
- Scanner
 - Reads the input words and enters states representing those words into the chart
- Completer
 - Moves the dot to the right when new constituents are found

Predictor

- Intuition:
 - Create new state for top-down prediction of new phrase
- Applied when non part-of-speech non-terminals are to the right of a dot:
 - $S \rightarrow \cdot VP$ [0,0]
- Adds new states to *current* chart
 - One new state for each expansion of the non-terminal in the grammar
 - $VP \rightarrow \cdot V$ [0,0]
 - $VP \rightarrow \cdot V NP$ [0,0]

Chart[0]

S0	$\gamma \rightarrow \cdot S$	[0,0]	Dummy start state
S1	$S \rightarrow \cdot NP VP$	[0,0]	Predictor
S2	$S \rightarrow \cdot Aux NP VP$	[0,0]	Predictor
S3	$S \rightarrow \cdot VP$	[0,0]	Predictor
S4	$NP \rightarrow \cdot Pronoun$	[0,0]	Predictor
S5	$NP \rightarrow \cdot Proper-Noun$	[0,0]	Predictor
S6	$NP \rightarrow \cdot Det Nominal$	[0,0]	Predictor
S7	$VP \rightarrow \cdot Verb$	[0,0]	Predictor
S8	$VP \rightarrow \cdot Verb NP$	[0,0]	Predictor
S9	$VP \rightarrow \cdot Verb NP PP$	[0,0]	Predictor
S10	$VP \rightarrow \cdot Verb PP$	[0,0]	Predictor
S11	$VP \rightarrow \cdot VP PP$	[0,0]	Predictor

Chart[1]

S12	Verb → book •	[0,1]	Scanner
S13	VP → Verb •	[0,1]	Completer
S14	VP → Verb • NP	[0,1]	Completer
S15	VP → Verb • NP PP	[0,1]	Completer
S16	VP → Verb • PP	[0,1]	Completer
S17	S → VP •	[0,1]	Completer
S18	VP → VP • PP	[0,1]	Completer
S19	NP → • Pronoun	[1,1]	Predictor
S20	NP → • Proper-Noun	[1,1]	Predictor
S21	NP → • Det Nominal	[1,1]	Predictor
S22	PP → • Prep NP	[1,1]	Predictor

Book that flight

S0: $\gamma \rightarrow \bullet S [0,0]$

γ
|
 $\bullet S$

Book that flight

S0: $\gamma \rightarrow \bullet S$ [0,0]

S3: $S \rightarrow \bullet VP$ [0,0]

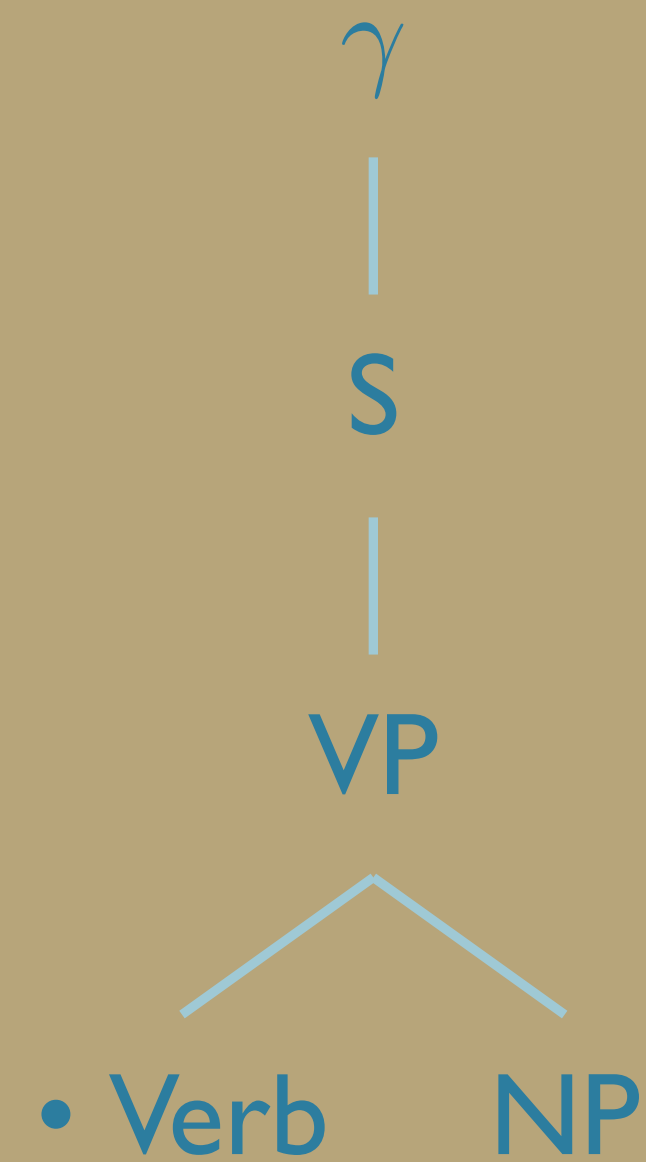
γ
|
S
|
 $\bullet VP$

Book that flight

S0: $\gamma \rightarrow \cdot S$ [0,0]

S3: $S \rightarrow \cdot VP$ [0,0]

S8: $VP \rightarrow \cdot \text{Verb NP}$ [0,0]



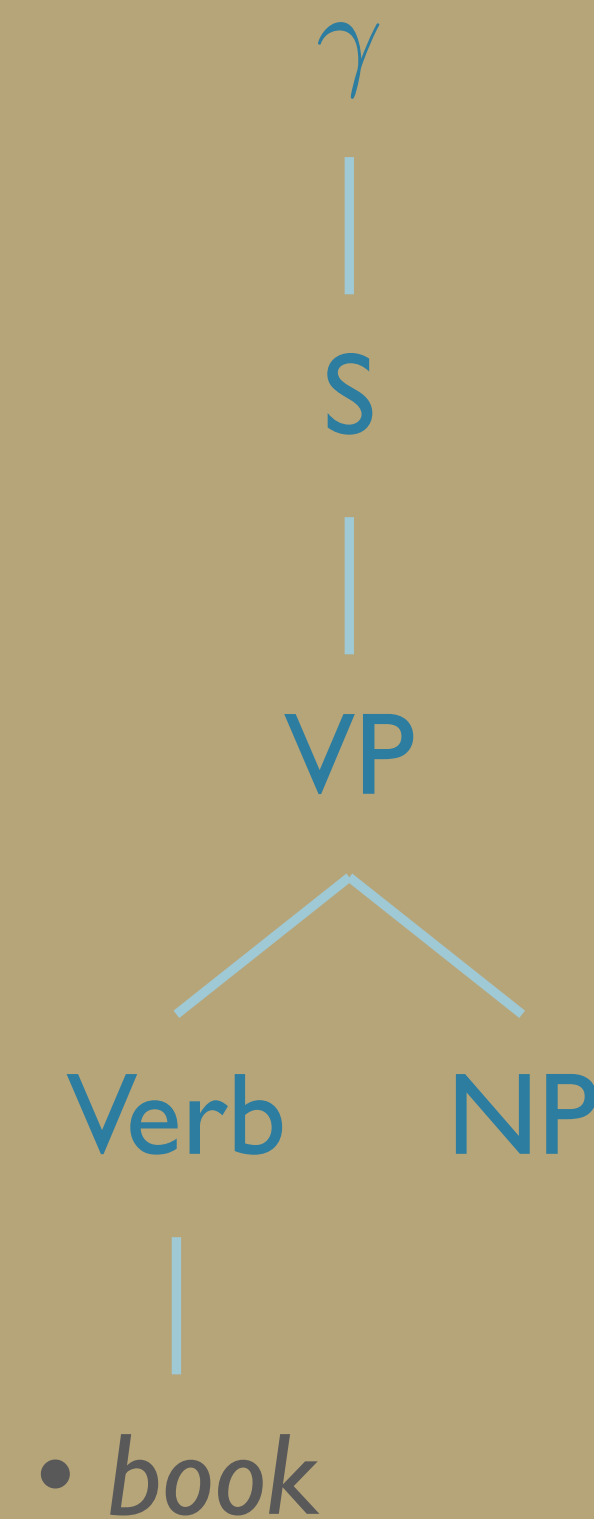
Book that flight

S0: $\gamma \rightarrow \cdot S$ [0,0]

S3: $S \rightarrow \cdot VP$ [0,0]

S8: $VP \rightarrow \cdot \text{Verb NP}$ [0,0]

S12: $\text{Verb} \rightarrow \cdot \text{book}$ [0,0]



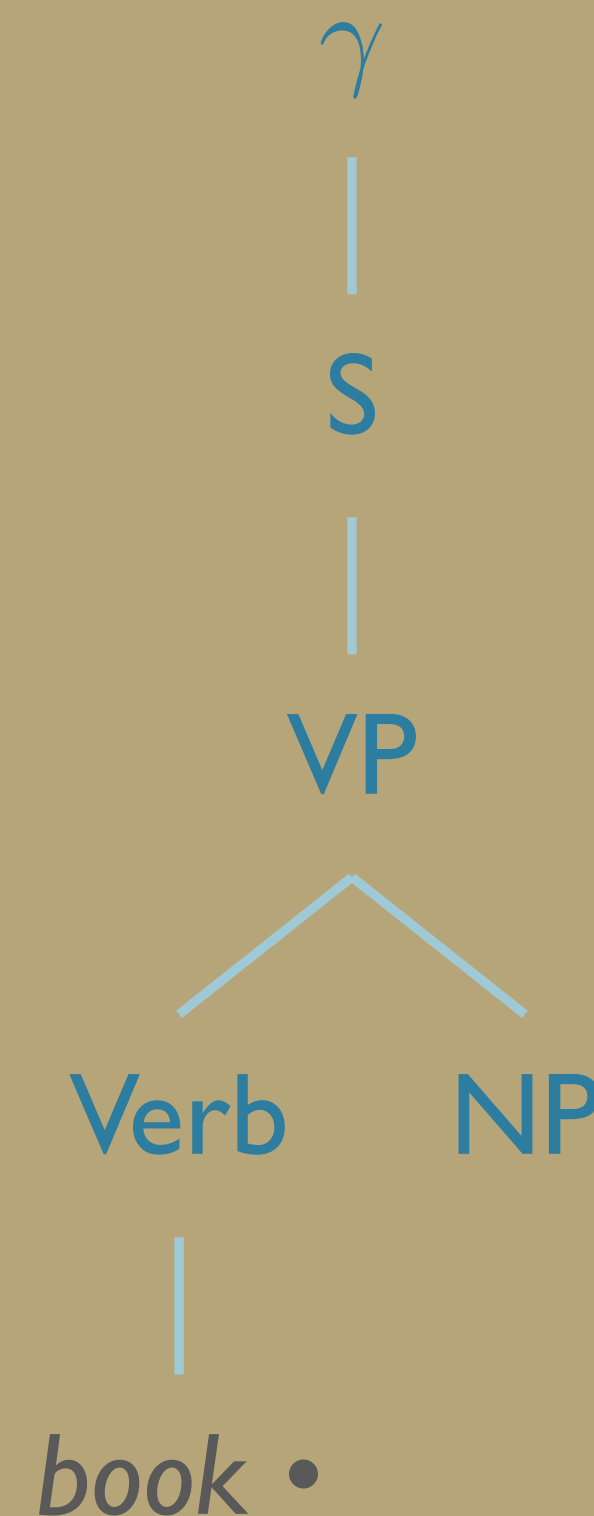
Book that flight

S0: $\gamma \rightarrow \cdot S$ [0,0]

S3: $S \rightarrow \cdot VP$ [0,0]

S8: $VP \rightarrow \cdot \text{Verb NP}$ [0,0]

S12: $\text{Verb} \rightarrow \text{book} \cdot$ [0,1]

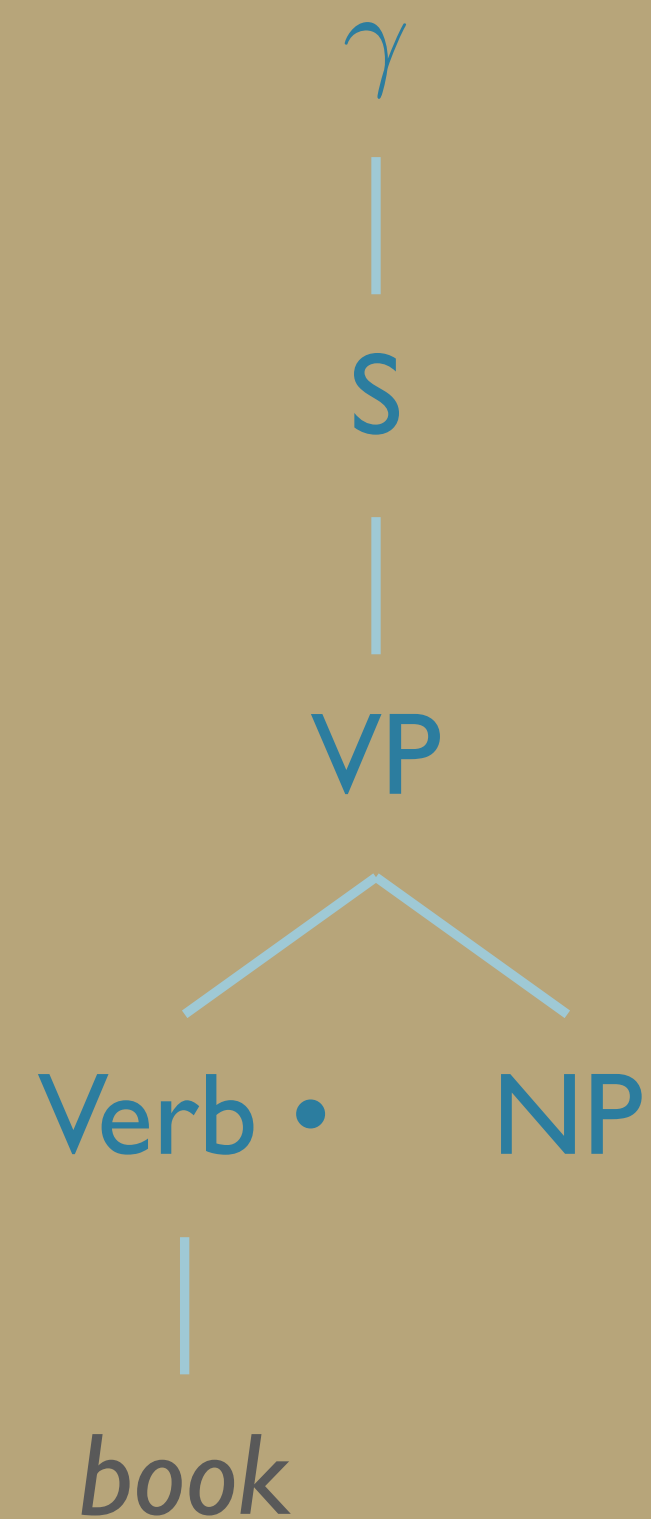


Book that flight

S0: $\gamma \rightarrow \cdot S$ [0,0]

S3: $S \rightarrow \cdot VP$ [0,0]

S8: $VP \rightarrow Verb \cdot NP$ [0,1]

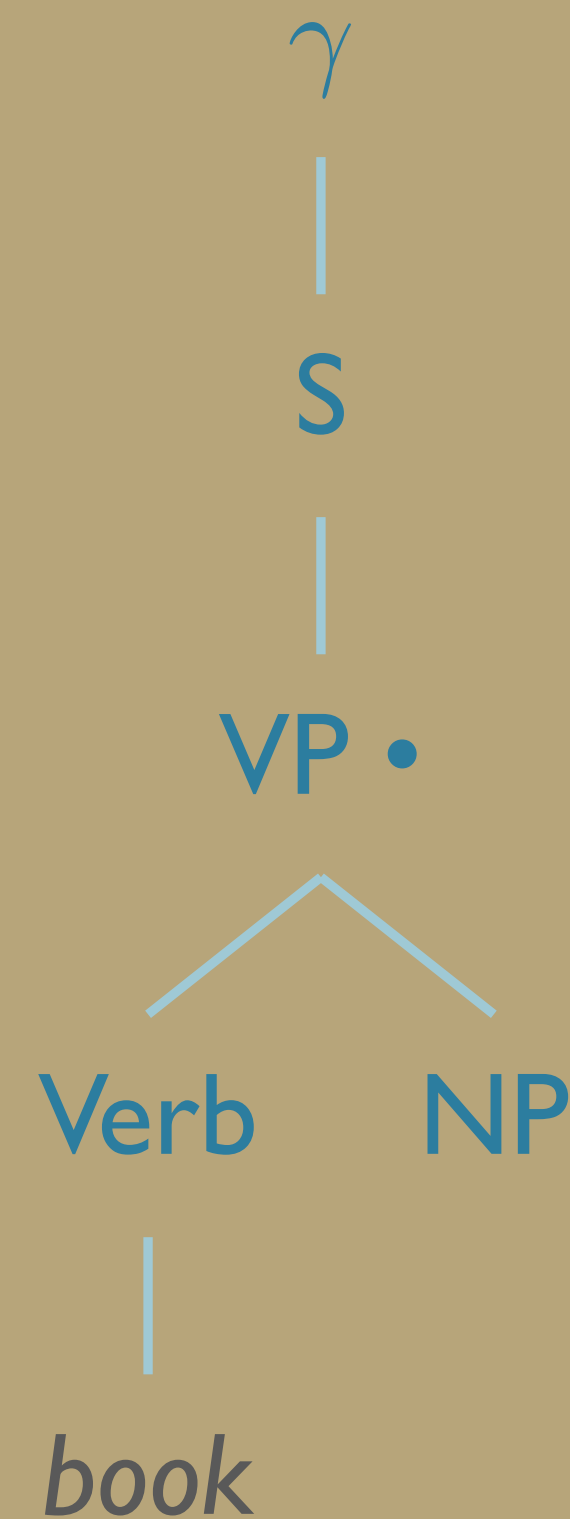


Book that flight

S0: $\gamma \rightarrow \cdot S$ [0,0]

S3: $S \rightarrow VP \cdot$ [0,1]

S8: $VP \rightarrow Verb \cdot NP$ [0,1]



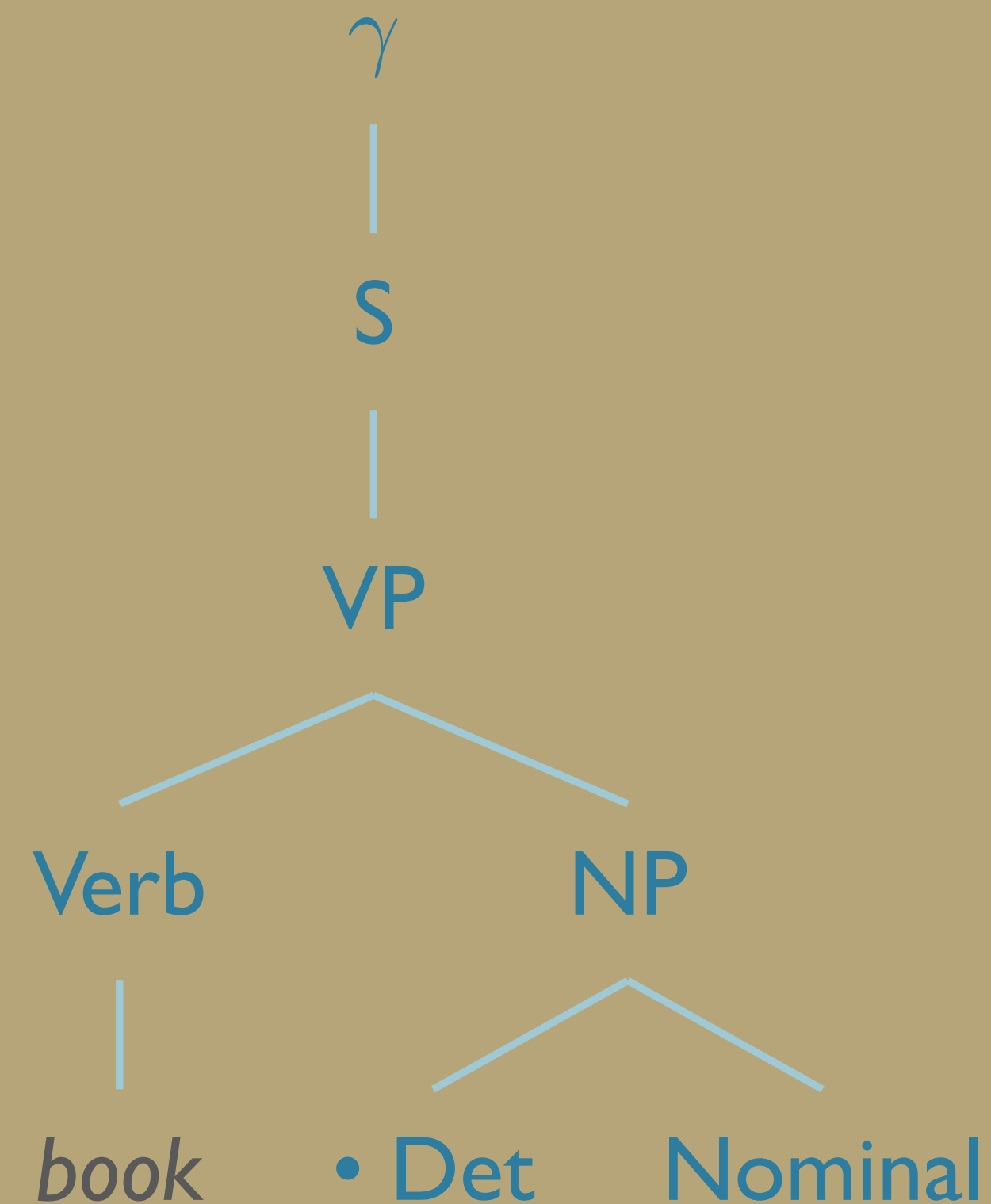
Book that flight

S0: $\gamma \rightarrow \cdot S$ [0,0]

S3: $S \rightarrow VP \cdot$ [0,1]

S8: $VP \rightarrow \text{Verb} \cdot \text{NP}$ [0,1]

S21: $\text{NP} \rightarrow \cdot \text{Det Nominal}$ [1,1]



Book that flight

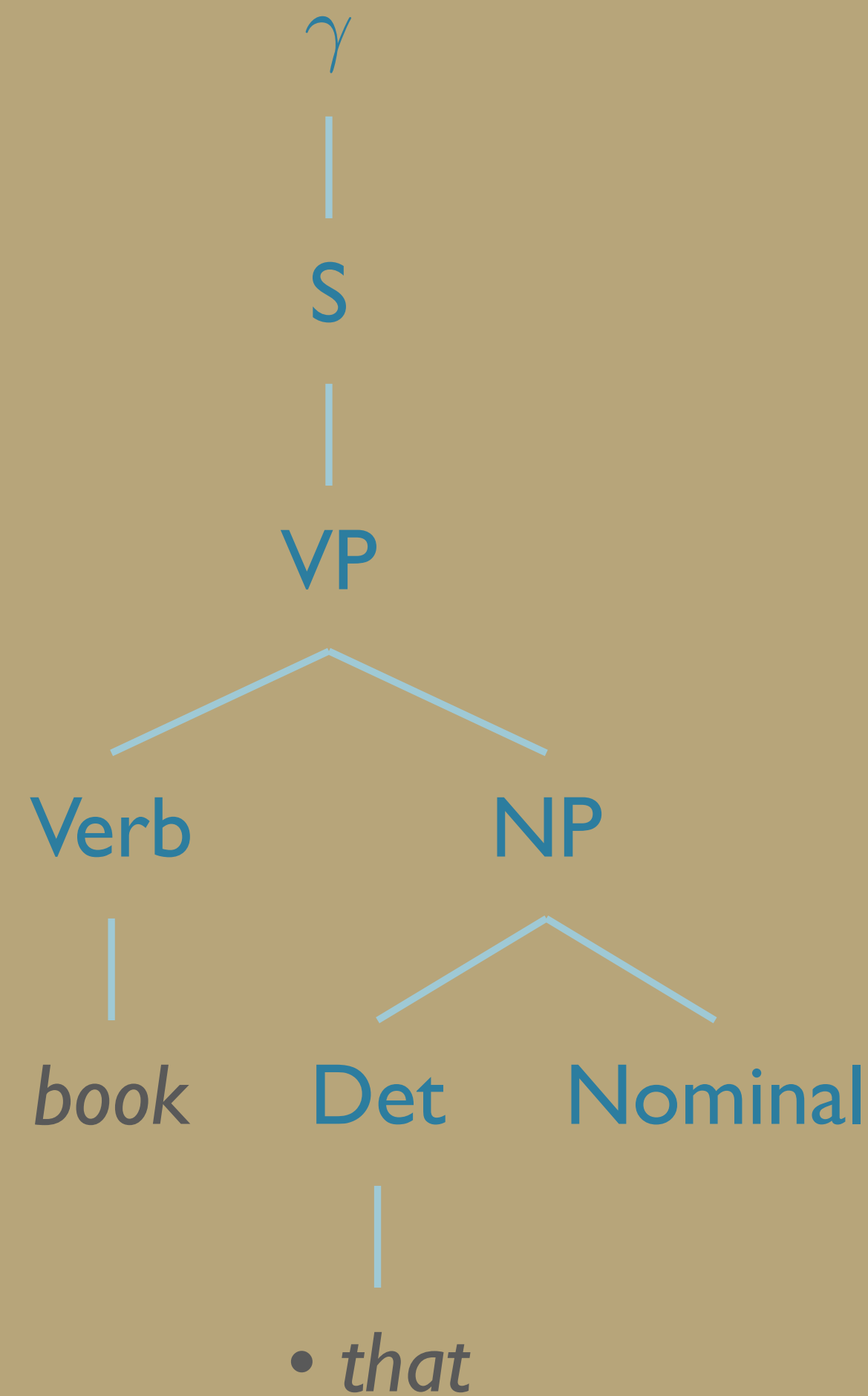
S0: $\gamma \rightarrow \cdot S$ [0,0]

S3: $S \rightarrow VP \cdot$ [0,1]

S8: $VP \rightarrow Verb \cdot NP$ [0,1]

S21: $NP \rightarrow \cdot Det\ Nominal$ [1,1]

S23: $Det \rightarrow \cdot \text{"that"}$ [1,1]



Book that flight

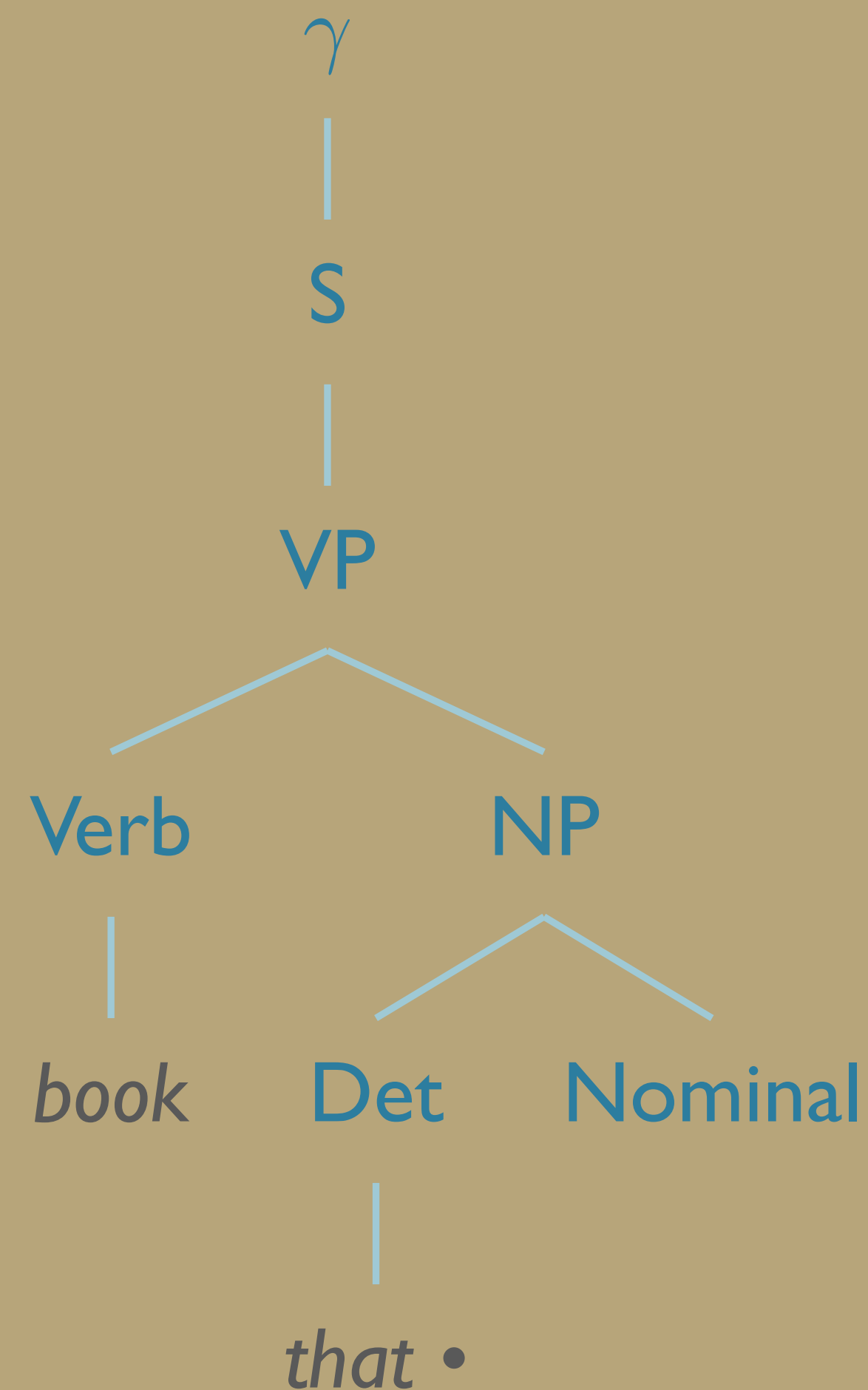
S0: $\gamma \rightarrow \cdot S$ [0,0]

S3: $S \rightarrow VP \cdot$ [0,1]

S8: $VP \rightarrow Verb \cdot NP$ [0,1]

S21: $NP \rightarrow \cdot Det\ Nominal$ [1,1]

S23: $Det \rightarrow \text{"that"} \cdot$ [1,2]



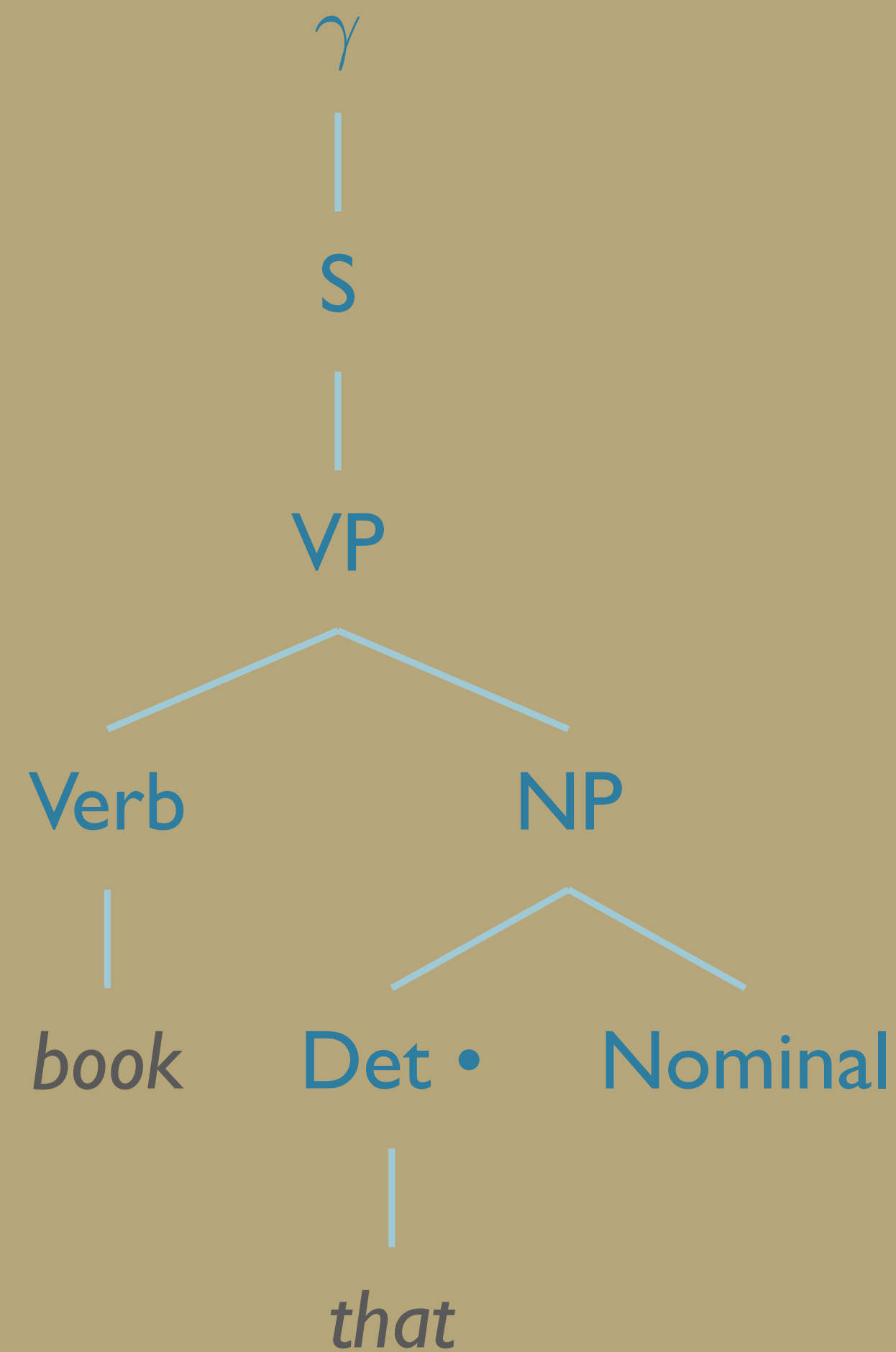
Book that flight

S0: $\gamma \rightarrow \cdot S$ [0,0]

S3: $S \rightarrow VP \cdot$ [0,1]

S8: $VP \rightarrow Verb \cdot NP$ [0,1]

S21: $NP \rightarrow Det \cdot Nominal$ [1,2]



Book that flight

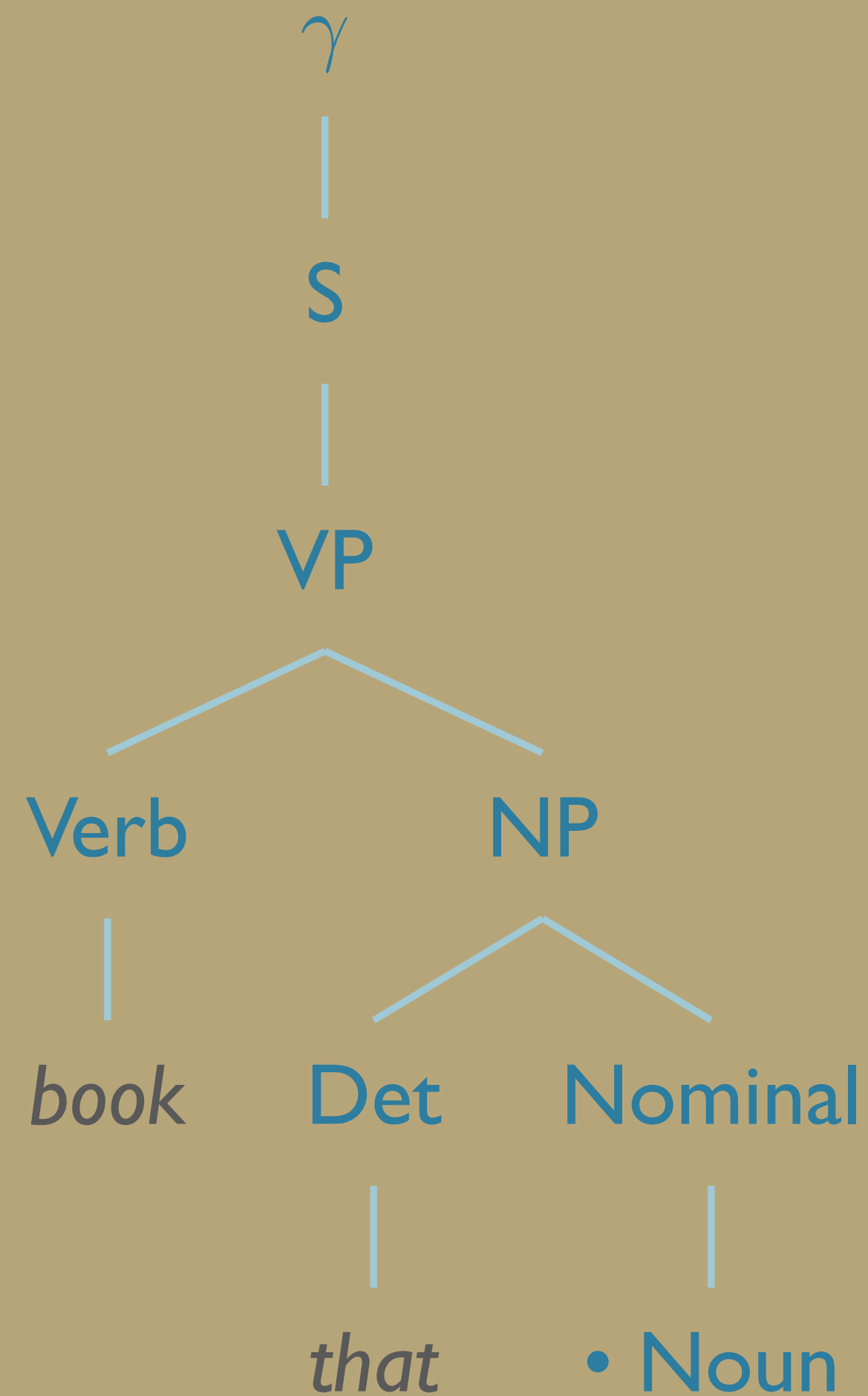
S0: $\gamma \rightarrow \cdot S$ [0,0]

S3: $S \rightarrow VP \cdot$ [0,1]

S8: $VP \rightarrow Verb \cdot NP$ [0,1]

S21: $NP \rightarrow Det \cdot Nominal$ [1,2]

S25: $Nominal \rightarrow \cdot Noun$ [2,2]



Book that flight

S0: $\gamma \rightarrow \cdot S$ [0,0]

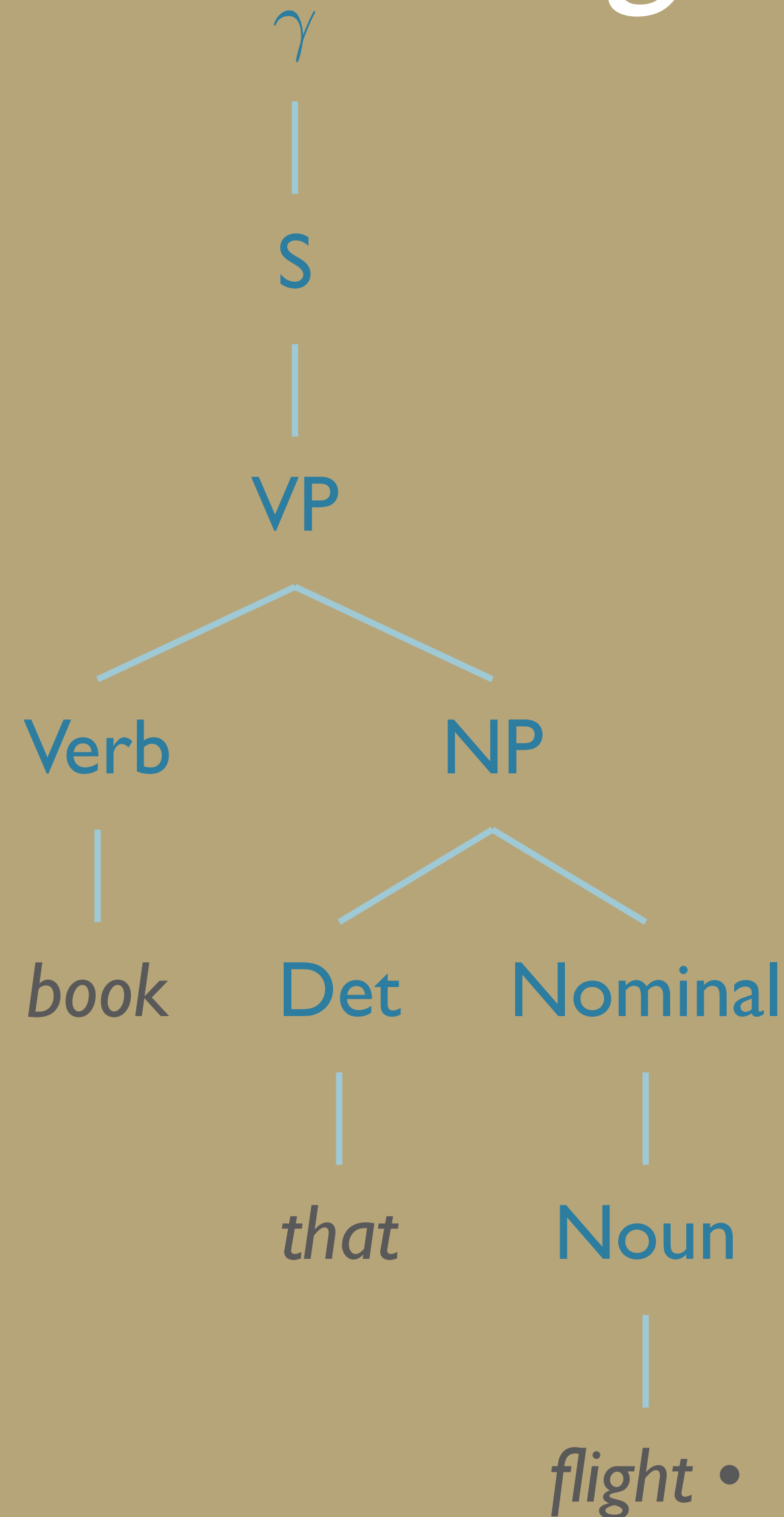
S3: $S \rightarrow VP \cdot$ [0,1]

S8: $VP \rightarrow Verb \cdot NP$ [0,1]

S21: $NP \rightarrow Det \cdot Nominal$ [1,2]

S25: $Nominal \rightarrow \cdot Noun$ [2,2]

S28: $Noun \rightarrow \text{"flight"} \cdot$ [2,3]



Book that flight

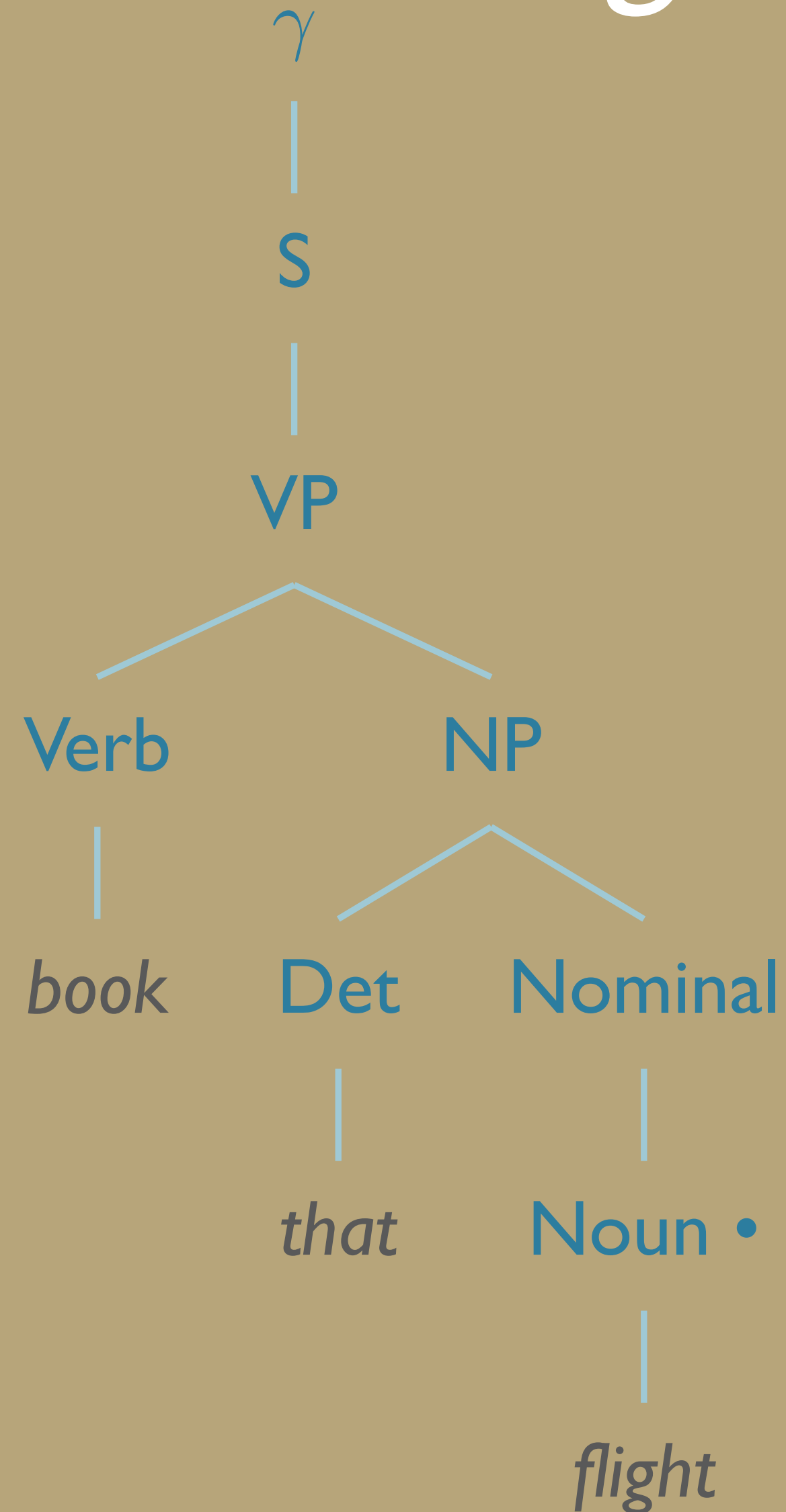
S0: $\gamma \rightarrow \cdot S$ [0,0]

S3: $S \rightarrow VP \cdot$ [0,1]

S8: $VP \rightarrow Verb \cdot NP$ [0,1]

S21: $NP \rightarrow Det \cdot Nominal$ [1,2]

S25: $Nominal \rightarrow Noun \cdot$ [2,3]



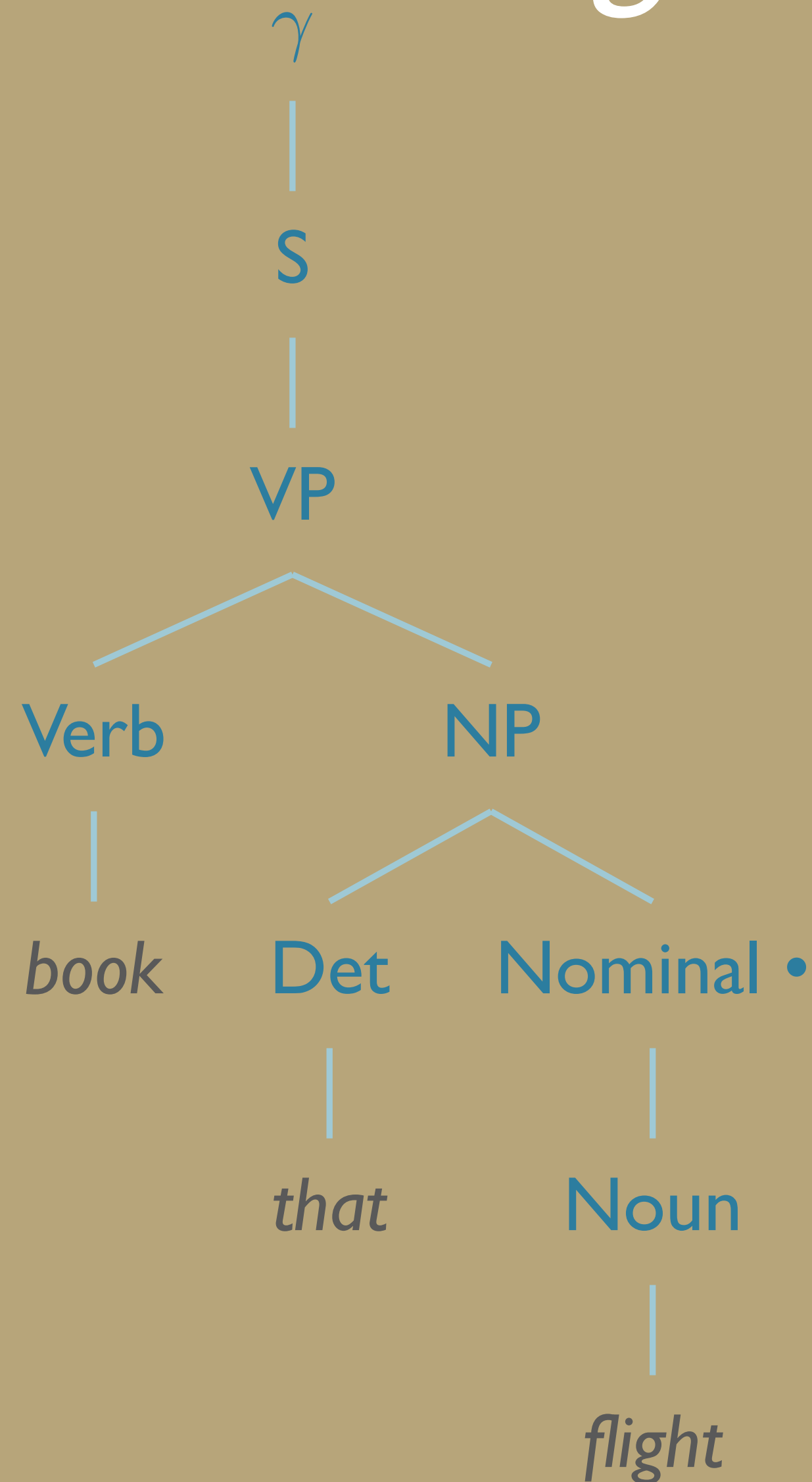
Book that flight

S0: $\gamma \rightarrow \cdot S$ [0,0]

S3: $S \rightarrow VP \cdot$ [0,1]

S8: $VP \rightarrow Verb \cdot NP$ [0,1]

S21: $NP \rightarrow Det\ Nominal \cdot$ [1,3]

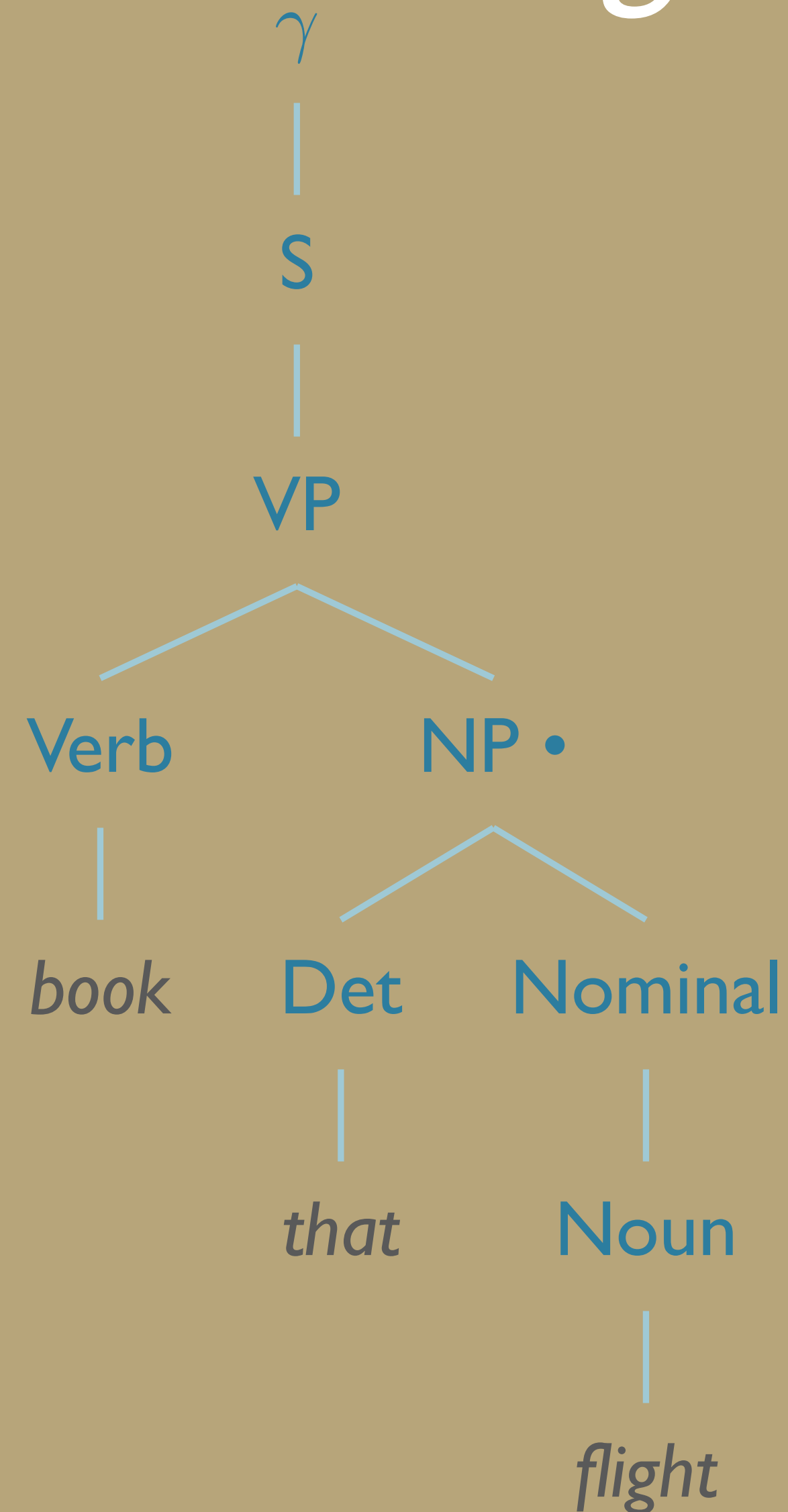


Book that flight

S0: $\gamma \rightarrow \cdot S$ [0,0]

S3: $S \rightarrow VP \cdot$ [0,1]

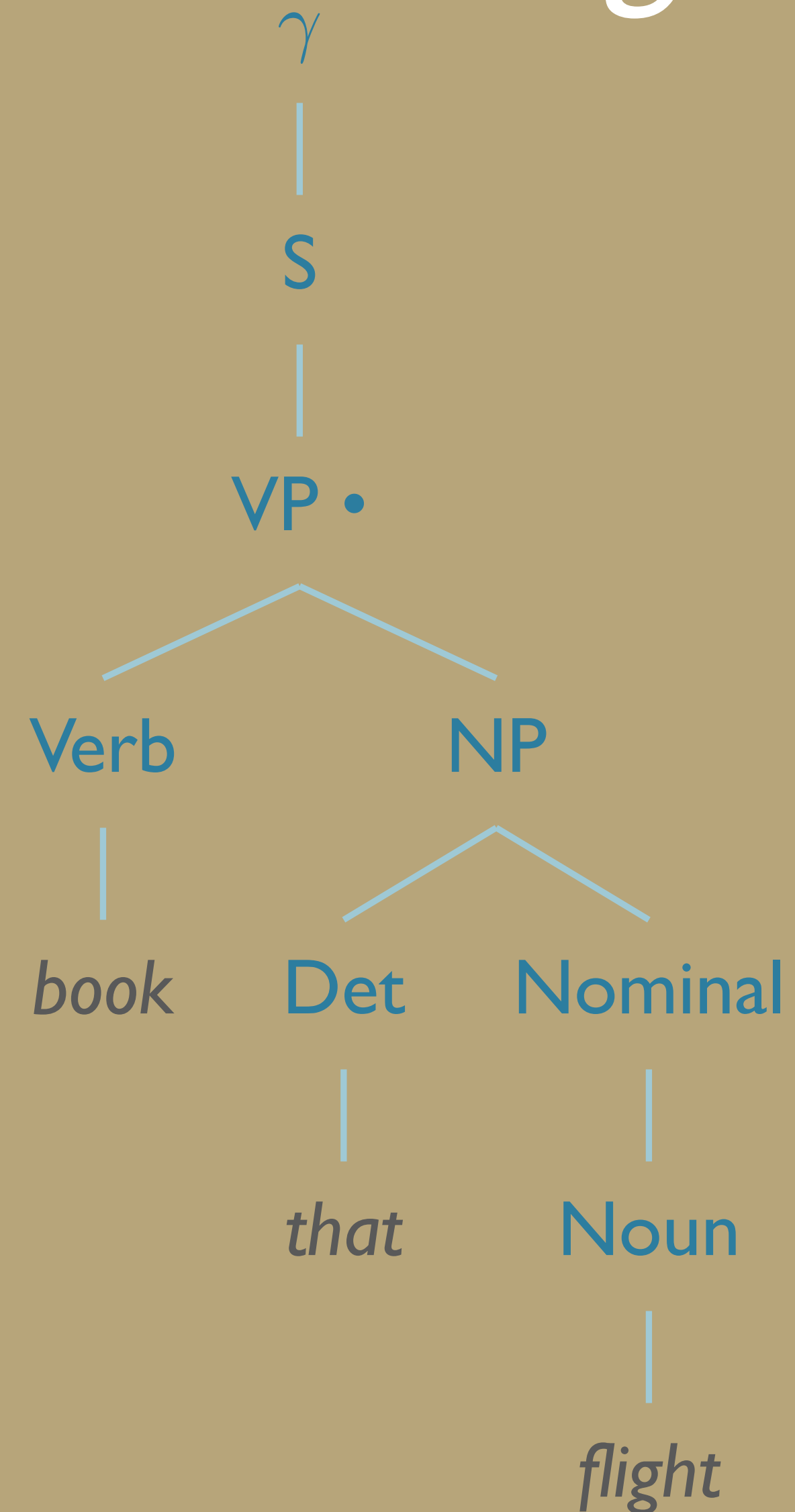
S8: $VP \rightarrow \text{Verb NP} \cdot$ [0,3]



Book that flight

S0: $\gamma \rightarrow \cdot S [0,0]$

S3: $S \rightarrow VP \cdot [0,3]$



What About Dead Ends?

Book that flight

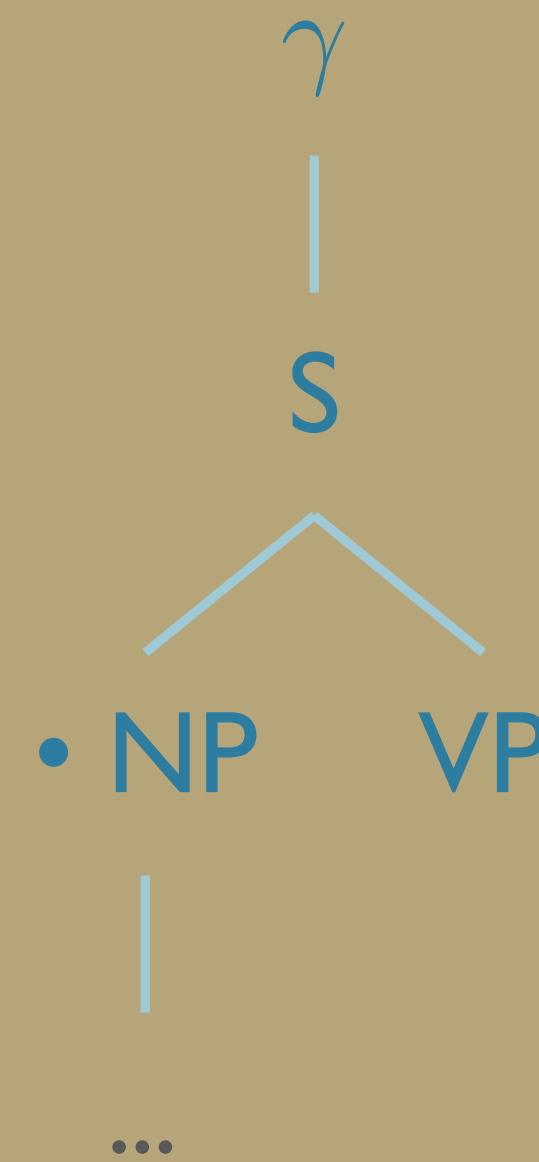
S0: $\gamma \rightarrow \bullet S$ [0,0]

S1: $S \rightarrow \bullet NP VP$ [0,0]

~~NP $\rightarrow \bullet$ Pronoun~~

~~NP $\rightarrow \bullet$ Proper-Noun~~

~~NP $\rightarrow \bullet$ Det Nominal~~



book

What About Recursion?

What about recursion?

- We now have a top-down parser in hand. Does it enter infinite loops on rules like $S \rightarrow S \text{ 'and' } S$?
- No!

```
procedure ENQUEUE(state, chart-entry)  
  if state is not already in chart-entry then  
    PUSH(state, chart-entry)  
  end
```

Exercise: parse 'table and chair' using the very simple grammar
 $\text{Nom} \rightarrow \text{Nom 'and' Nom} \mid \text{'table'} \mid \text{'chair'}$

HW #3

CKY Parsing: Goals

- Complete implementation of CKY parser
- Implement dynamic programming approach
- Incorporate/follow backpointers to recover parse

Implementation

- Build full parser
- Can use any language, per course policies
- You may use existing data structures for rules, trees
 - e.g. NLTK has nice `tree` data structure
 - CKY algorithm must be your own
- Dynamic programming table filling crucial!
- Will use smaller grammar (similar to HW #1)
- Back to ATIS for HW #4

Implementation

- For CKY Implementation:
 - NLTK's `CFG.productions()` method:
 - optional `rhs=` argument *only looks at first token of RHS*

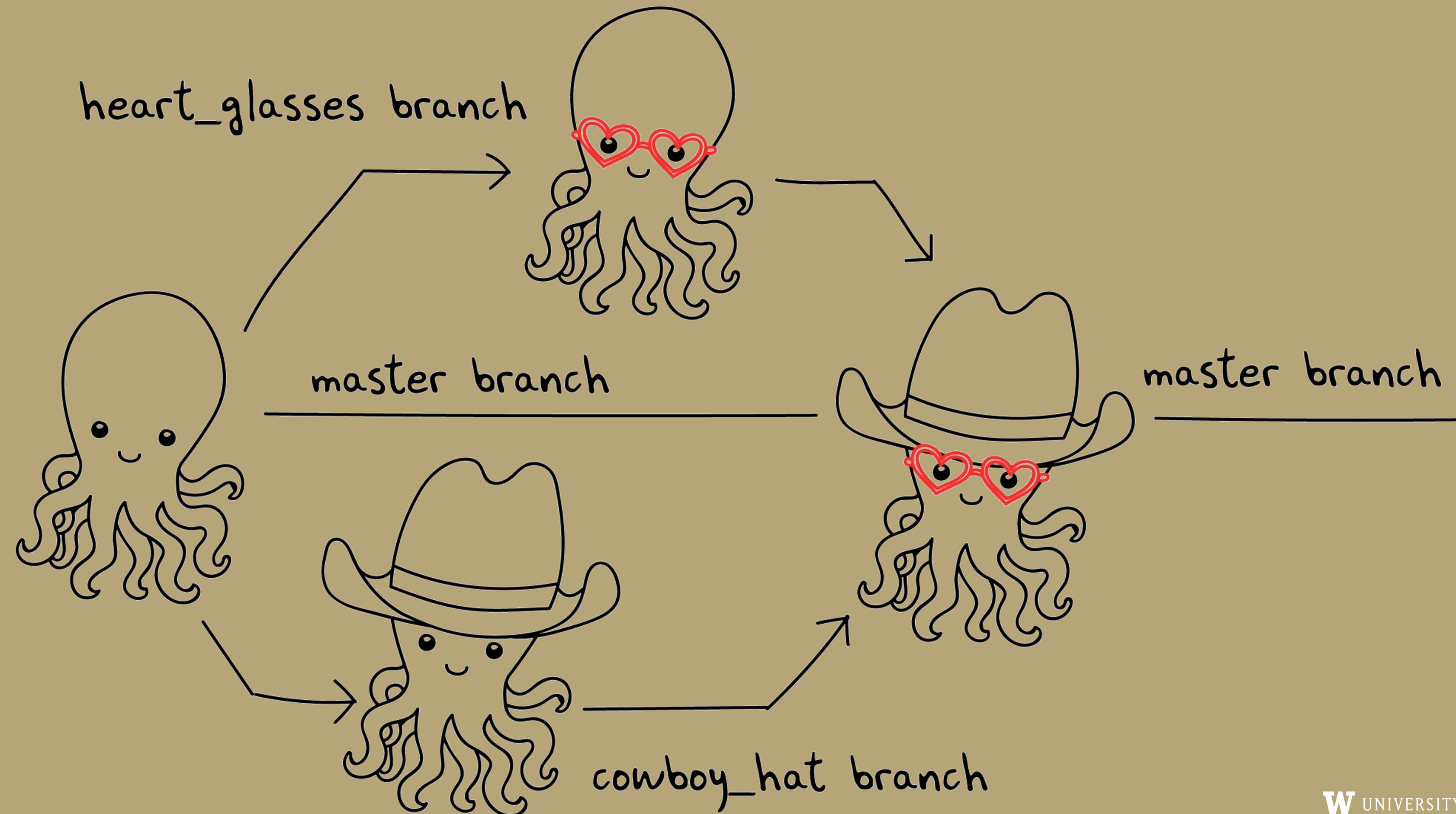
Notes

- Teams:
 - You may work in teams of two on this assignment
- Test grammar
 - Pre-converted to CNF
 - Start symbol: **TOP**
 - Parse should span input and be rooted at: **TOP**

Some Collaboration Basics

Git Branches

- Good for semi-isolating your development code from the shared, reviewed code



Recommended Git Flow

- Initialize a git repository, with a `master` branch
 - (Create initial checkin, if necessary)
- Create a new branch, maybe “`adding_rule_objects`”
- Make regular checkins on your branch (like saving)
- Switch to `master` branch, and “pull”
- Merge your branch to master
- ...rinse & repeat
- If using GitHub (or GitLab, etc): **MUST BE PRIVATE REPO!**

Communication: Check-ins

- For check-ins, three main points:
 - What have you been working on?
 - What do you plan to work on next?
 - Is there anything “blocking” you?
- In industry, these brief check-ins among small teams are often done daily

Project Planning: Kanban Boards

- Before you start working:
 - Write out tasks on sticky notes.
 - Place in three columns:
 - To-Do
 - Doing
 - Done
 - As you work, you can move them from column to column
 - Add tasks as new issues come up
- trello.com – has free online implementation of Kanban Boards

